

Nucleon Structure at Jefferson Lab

I) the 6 GeV findings

Rolf Ent, 12th HANUC Lecture Week, Mar. 25, 2009

- The Role of Quarks in Nuclear Physics
CEBAF's Original Mission Statement
- **Nucleon and Pion Elastic Form Factors** and
Transition Form Factors to Nucleon Excited States
- The **Strange Quark Content** of the Proton
- The Onset of the **Quark Parton Model**:
The Quark-Hadron Transition
- **Deep Exclusive Reactions**:
Constraints on Angular Momentum
Proton Tomography

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Key Mission and Principal Focus (1987):

The study of the largely unexplored transition between the nucleon-meson and the quark-gluon descriptions of nuclear matter.

The Role of Quarks in Nuclear Physics

Related Areas of Study:

- Do individual nucleons change their size, shape, and quark structure in the nuclear medium?

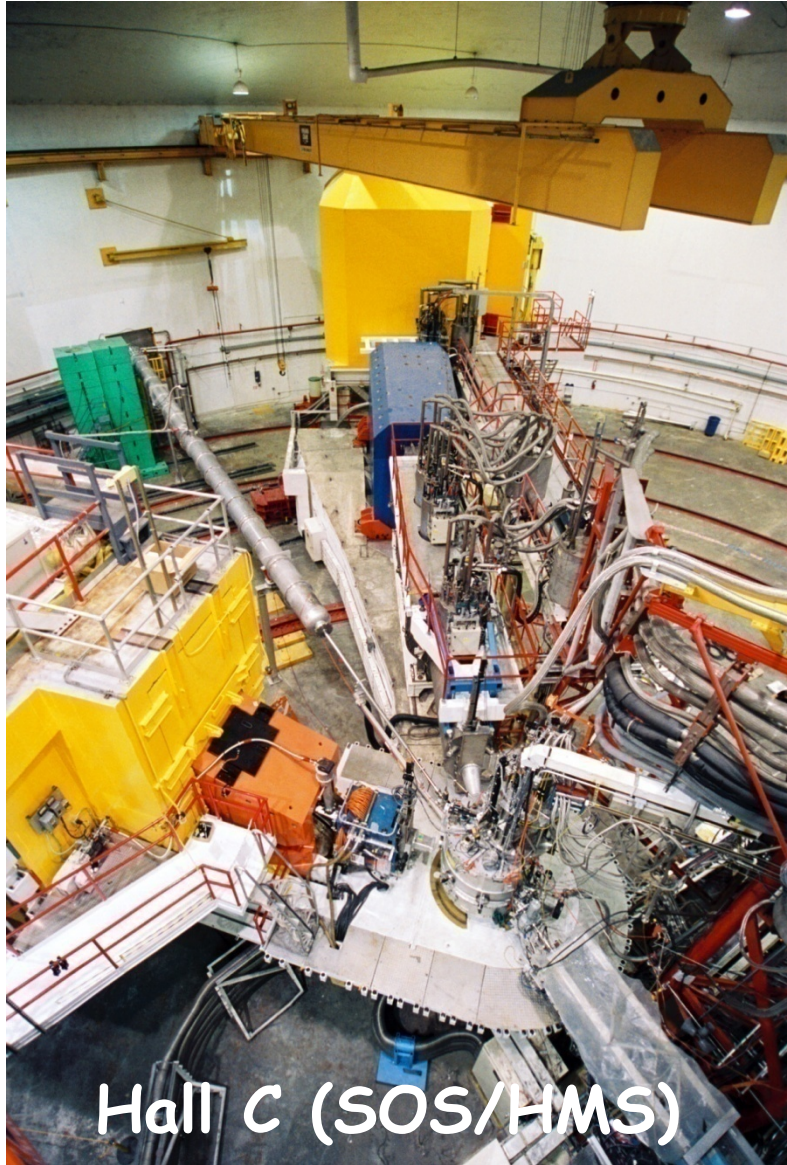
- How do nucleons cluster in the nuclear medium?

Pushing the Limits of the Standard Model of Nuclear Physics

- What are the properties of the force which binds quarks into nucleons and nuclei at distances where this force is strong and the quark confinement mechanism is important?

*Charge and Magnetization in Nucleons and Pions
The Onset of the Parton Model*

Halls A/B/C Base Equipment



Hall B - *CLAS* (forward carriage and side clamshells retracted)

CLAS has more than 38,000 readout channels

Large angle EC

Panel 4 TOF

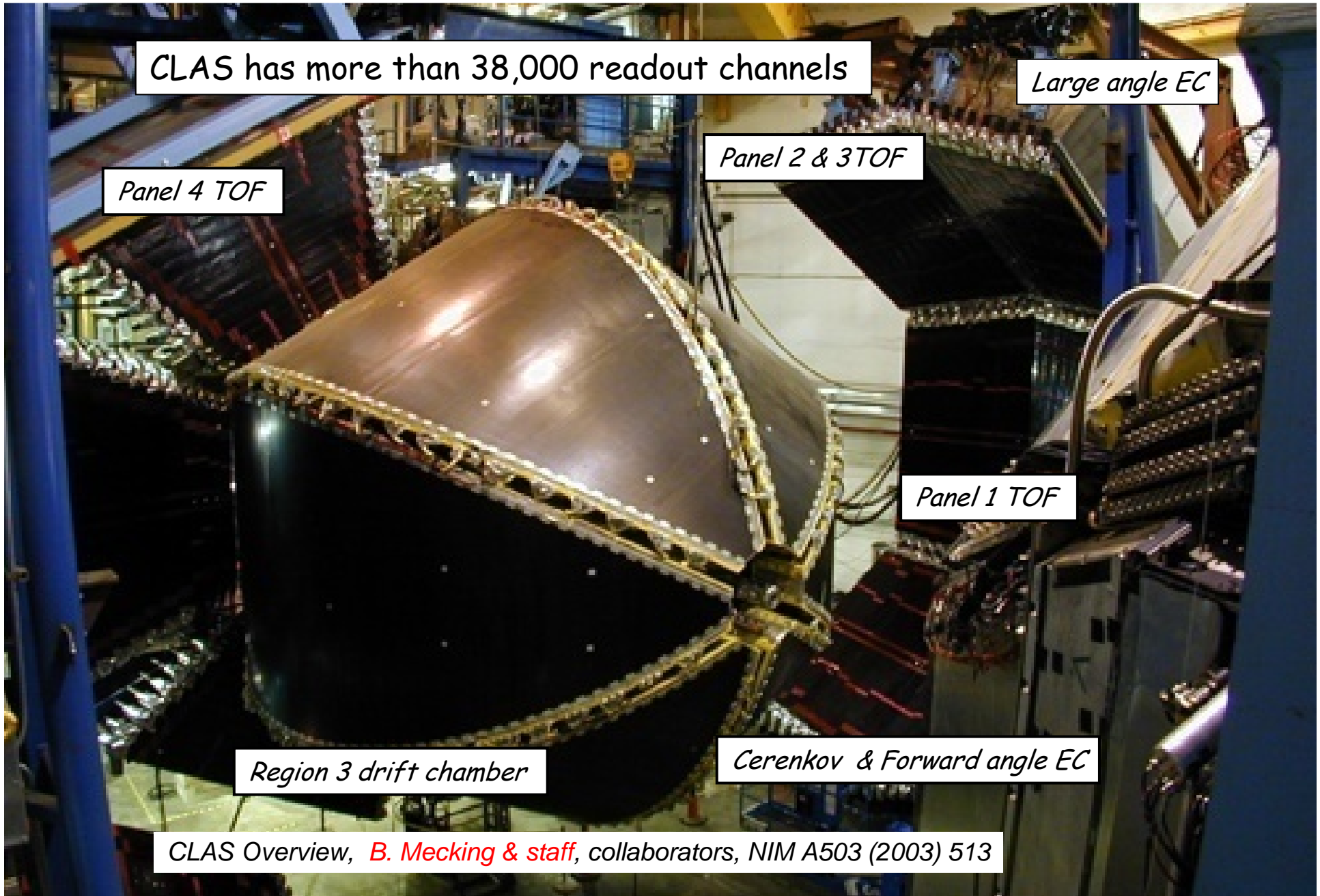
Panel 2 & 3 TOF

Panel 1 TOF

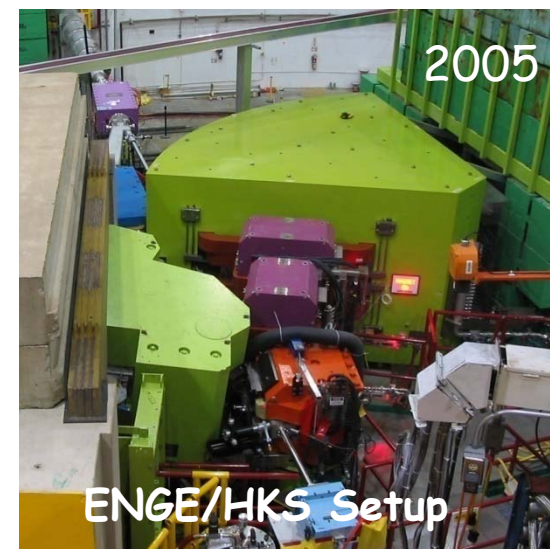
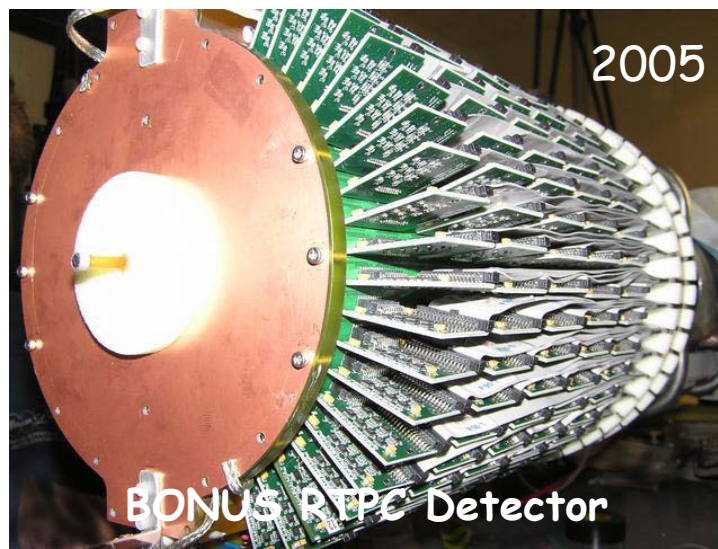
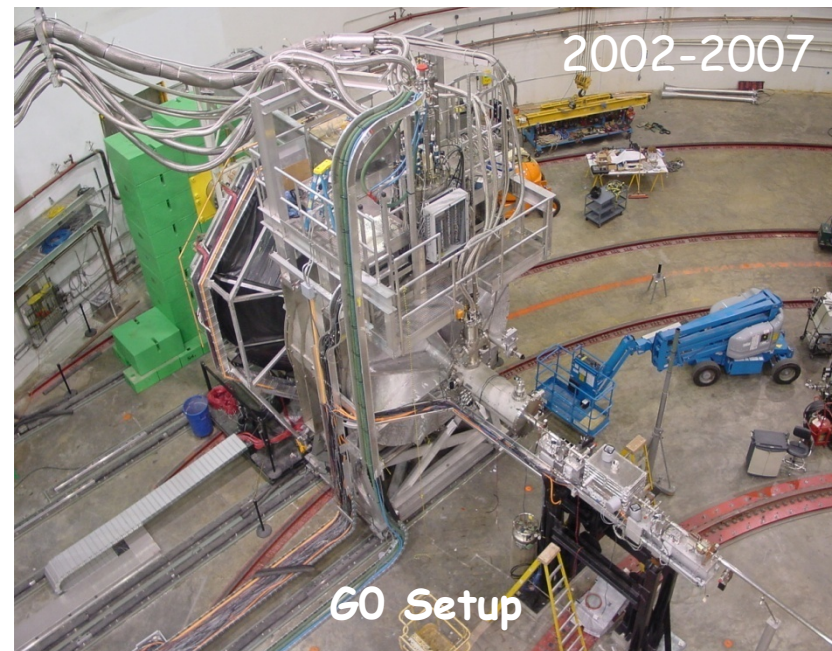
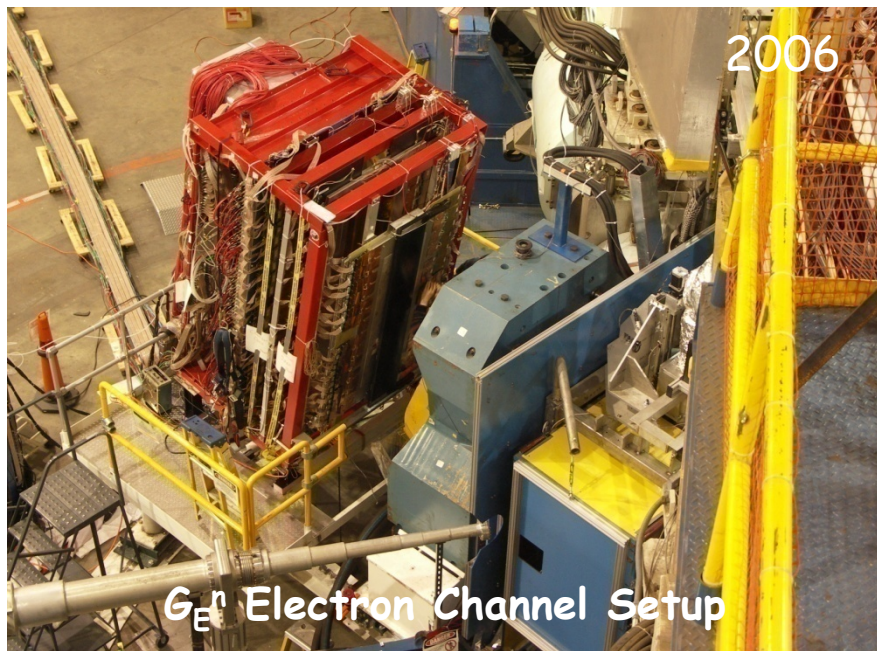
Region 3 drift chamber

Cerenkov & Forward angle EC

CLAS Overview, *B. Mecking & staff*, collaborators, NIM A503 (2003) 513



Ancillary Equipment and Experiment-Specific Apparatus



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Pushing the Limits of the Standard Model of Nuclear Physics

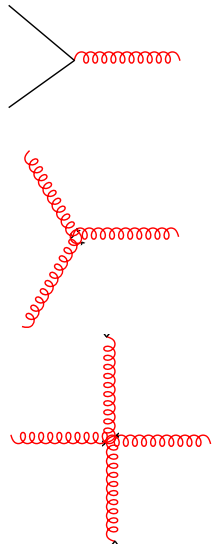
- What are the properties of the force which binds quarks into nucleons and nuclei at distances where this force is strong and the quark confinement mechanism is important?

Charge and Magnetization in Nucleons and Pions

The Onset of the Parton Model

QCD and Nuclei

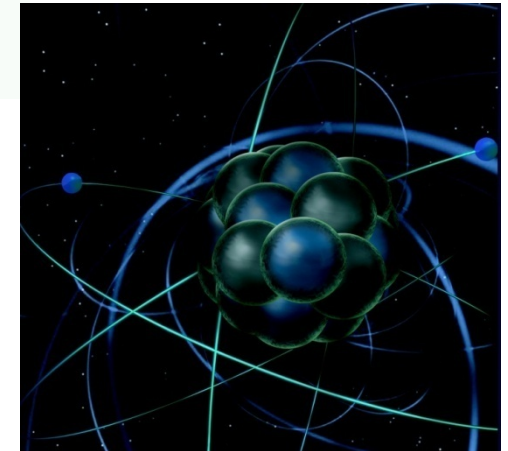
Gluons mediate the strong (color) force, just like photons mediate the electromagnetic force, but ... gluons interact with themselves ... which gives QCD unique properties



$$L_{QCD} = -\frac{1}{4}F^{a\mu\nu}F_{\mu\nu}^a + \sum_j \bar{q}_j(i\gamma^\mu D_\mu - m_j)q_j$$

$$F_{\mu\nu}^a \equiv \delta_\mu A_\nu^a - \delta_\nu A_\mu^a - gf^{abc}A_\mu^b A_\nu^c$$

$$D_\mu \equiv \delta_\mu + igA_\mu^a \frac{\lambda_a}{2}$$

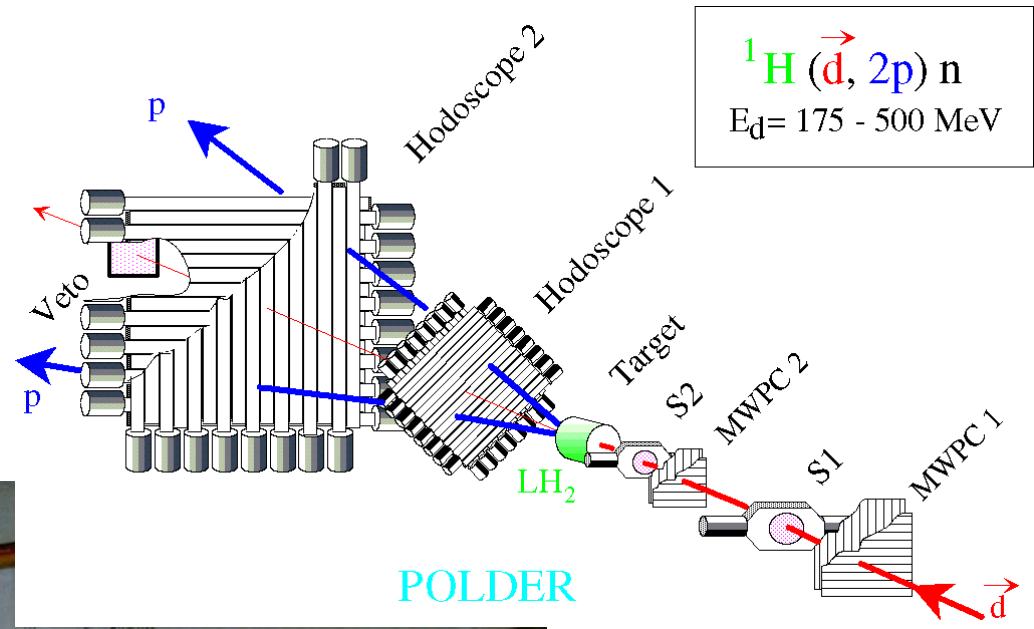


QCD Lagrangian: quarks and gluons

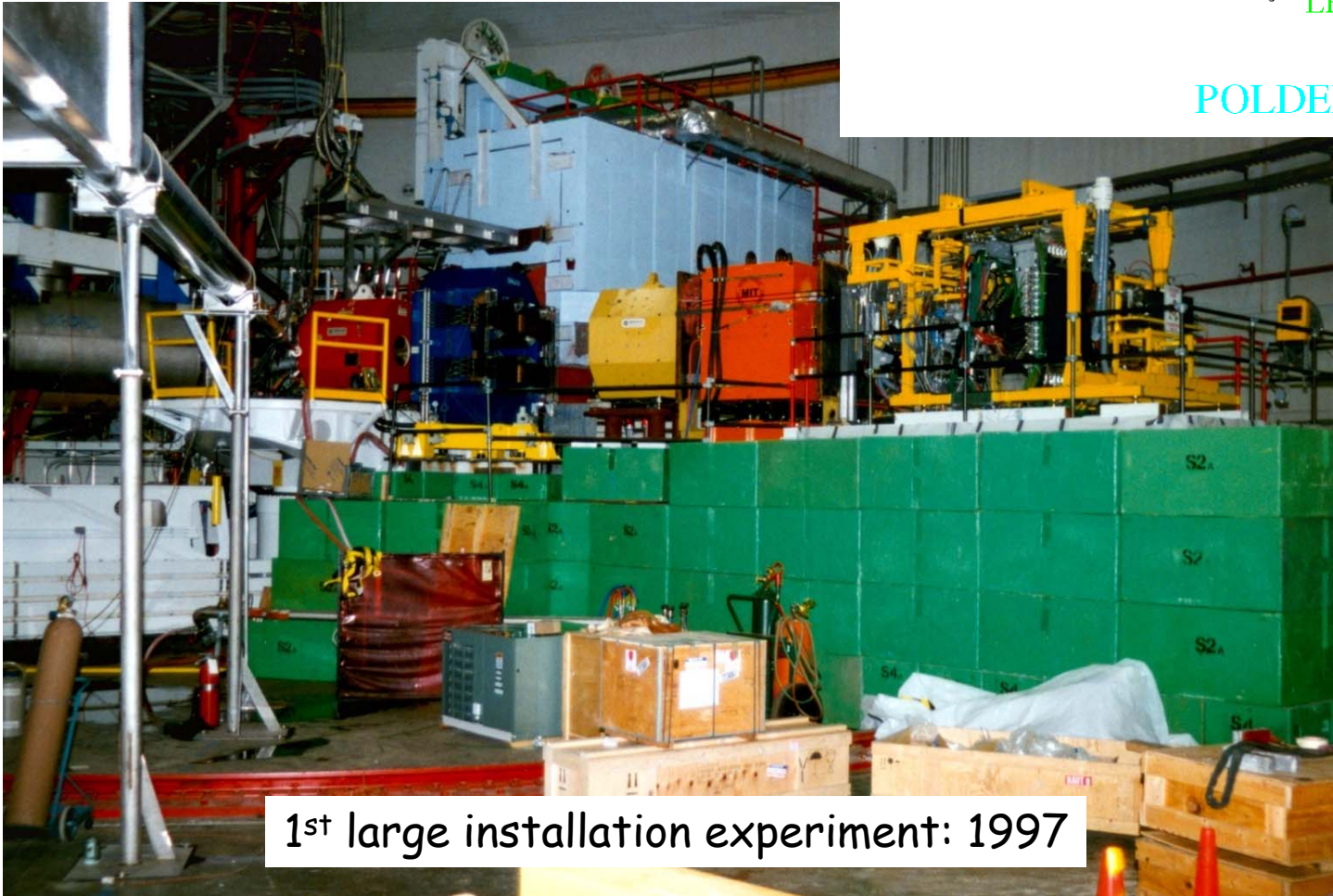
Nuclear Physics Model is an effective (but highly successful!) model using free nucleons and mesons as degrees of freedom.

${}^2\text{H}(e,e){}^2\text{H}$ elastic scattering
 ${}^2\text{H}$: spin-1 \rightarrow 3 form factors
 to disentangle

Solution: measure tensor
 polarization in ${}^2\text{H}(e,e'd)$



${}^1\text{H}(\vec{d}, 2p)n$
 $E_d = 175 - 500 \text{ MeV}$

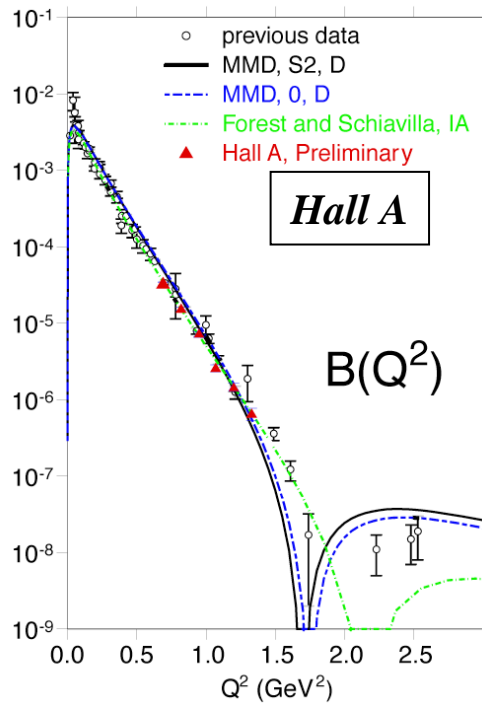
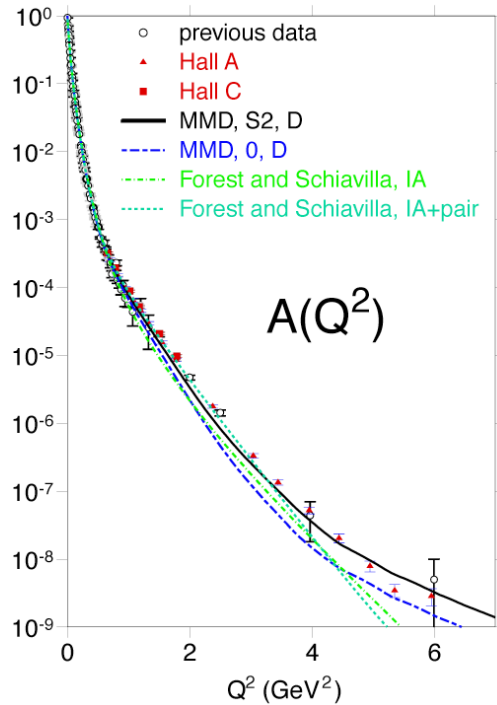


"T20 experiment"
 used HMS to detect
 the scattered
 electrons and a
 dedicated magnetic
 spectrometer on the



floor to
 detect the recoiling
 deuteron and
 measure its tensor
 polarization

JLab Data Reveal Deuteron's Size and Shape



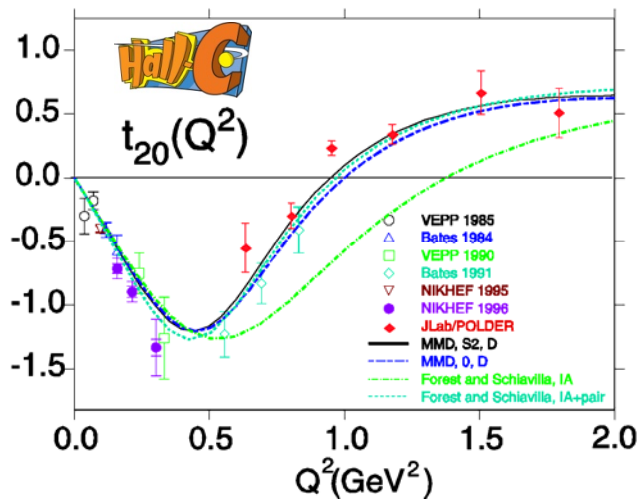
For elastic e-d scattering:

$$\frac{d\sigma}{d\Omega} = \sigma_M \left[A + B \tan^2 \frac{\theta}{2} \right]$$

$$A(Q^2) = G_C^2 + \frac{8}{9} \tau^2 G_Q^2 + \frac{2}{3} \tau G_M^2$$

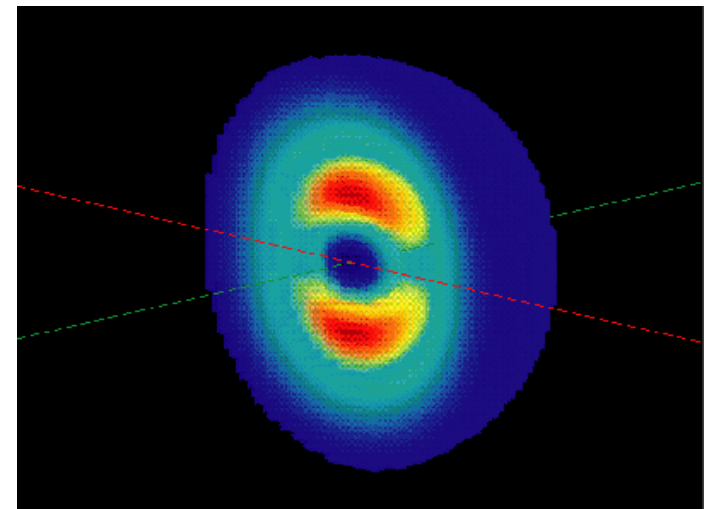
$$B(Q^2) = \frac{4}{3} \tau(1 + \tau) G_M^2$$

- 3rd observable needed to separate G_C and G_Q
- *tensor polarization t_{20}*



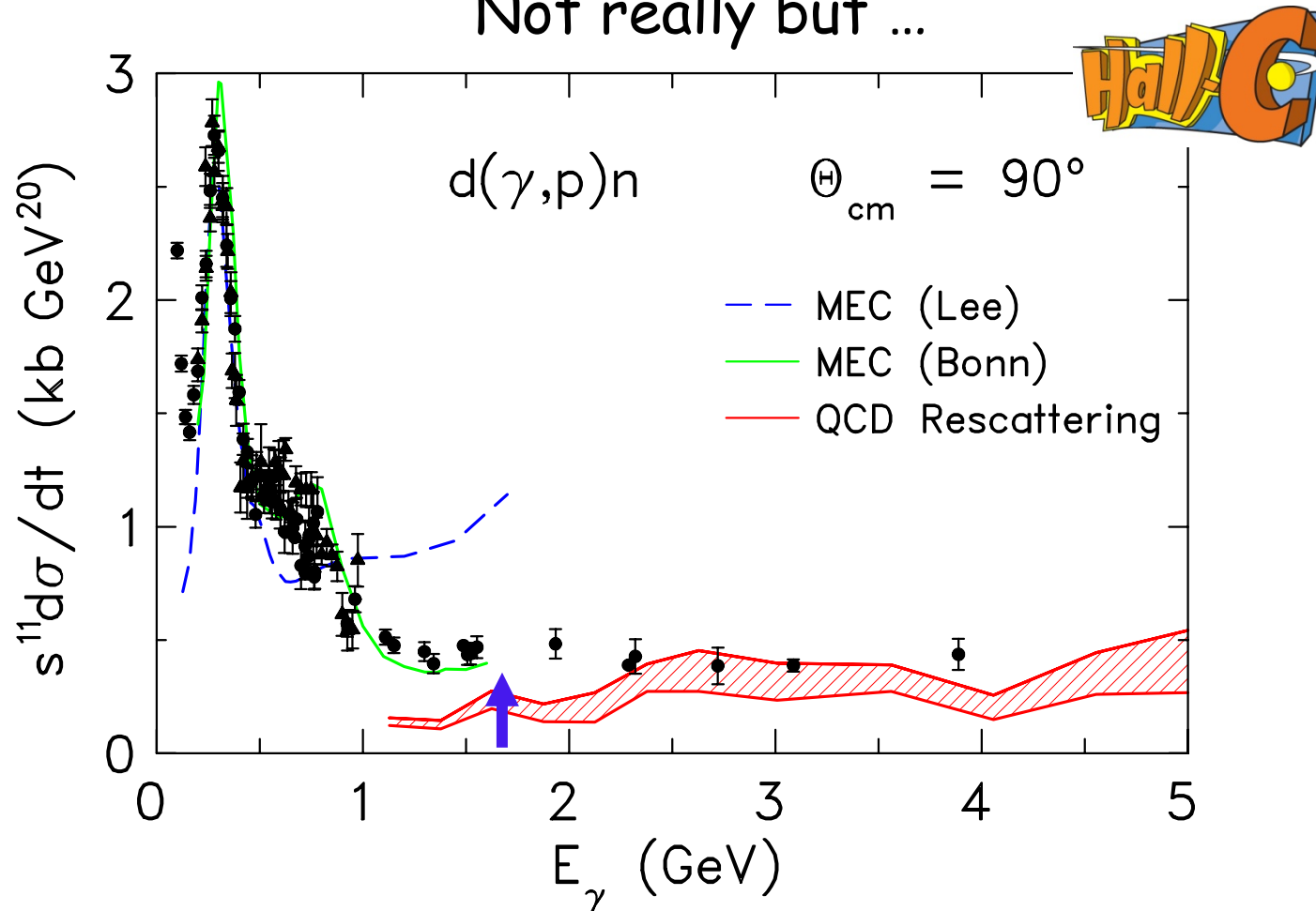
Combined Data →
 Deuteron's
 Intrinsic Shape

The nucleon-based
 description works
 down to < 0.5 fm



Is there a Limit for Meson-Baryon Models?

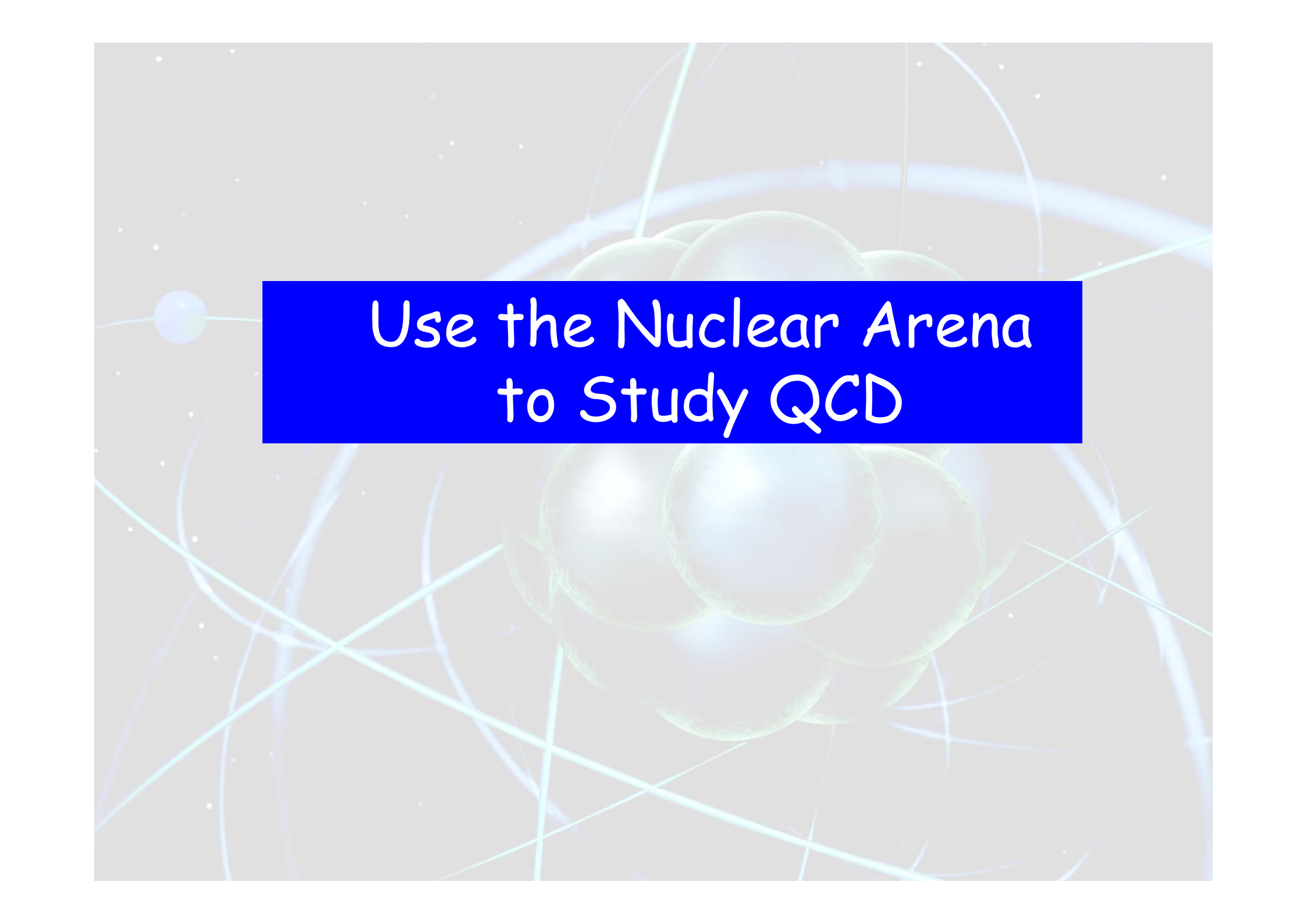
Not really but ...



... there might be a **more economical** QCD description.

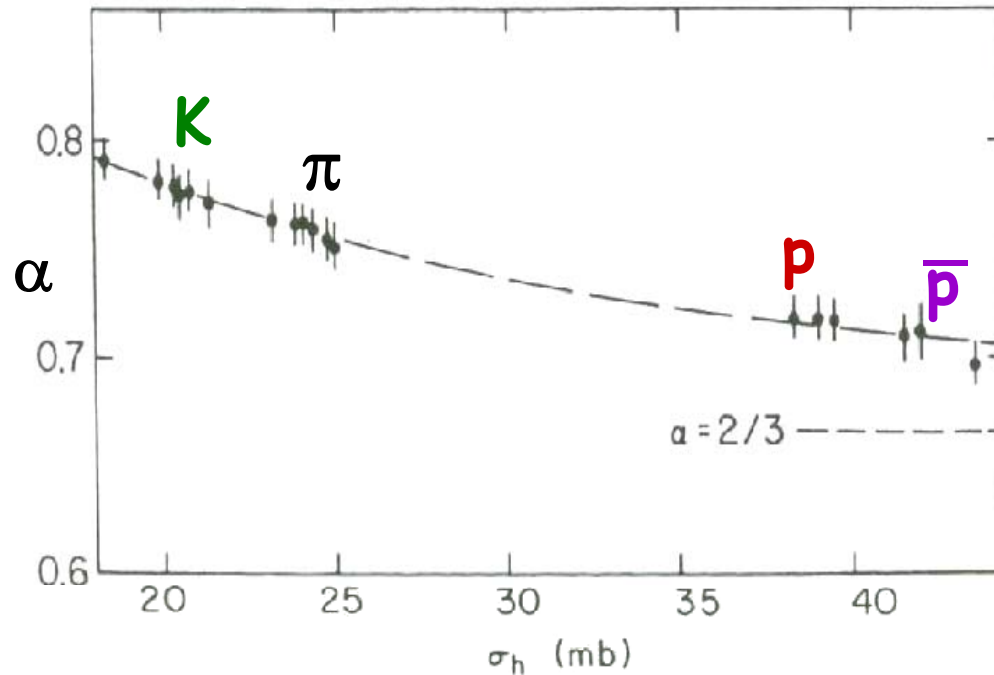
Scaling behavior ($d\sigma/dt \propto s^{-11}$)
 for $P_T > 1.2 \text{ GeV}/c$ (see \uparrow)

quark-gluon description
 sets



Use the Nuclear Arena
to Study QCD

Total Hadron-Nucleus Cross Sections



Hadron- Nucleus
total cross section

Fit to $\sigma(A) = \sigma_0 A^\alpha$

Hadron momentum
60, 200, 250 GeV/c

$$\alpha = 0.72 - 0.78, \text{ for } p, \pi, k$$

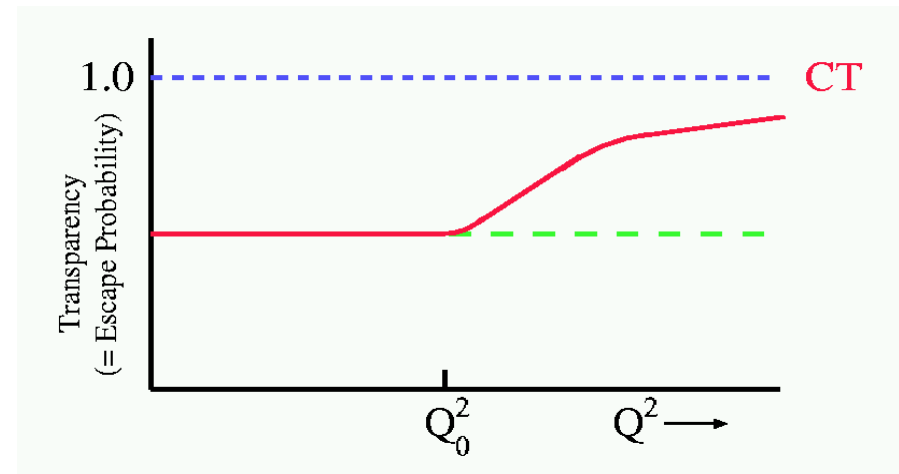
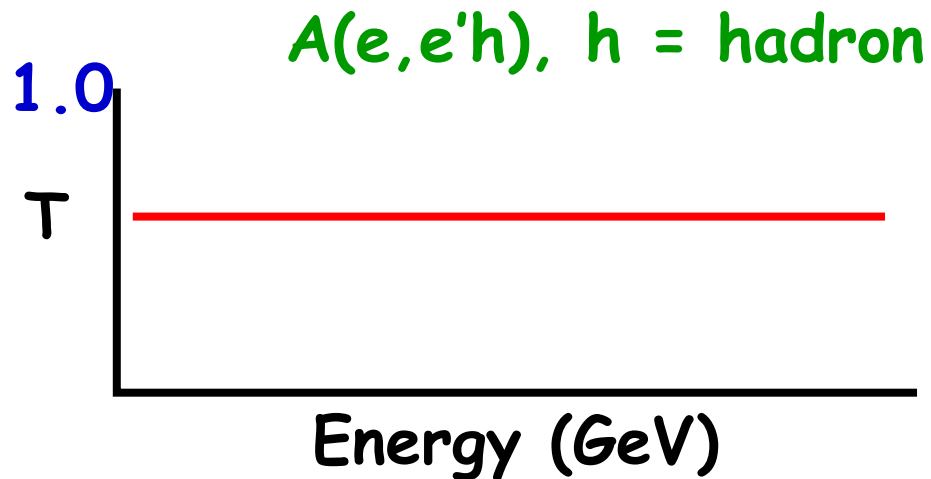
$\alpha < 1$ interpreted as due to the
strongly interacting nature of the
probe

A. S. Carroll *et al.* Phys. Lett 80B 319 (1979)

Physics of Nuclei: Color Transparency

Traditional nuclear physics expectation:
transparency **nearly energy independent**.

Quantum ChromoDynamics:



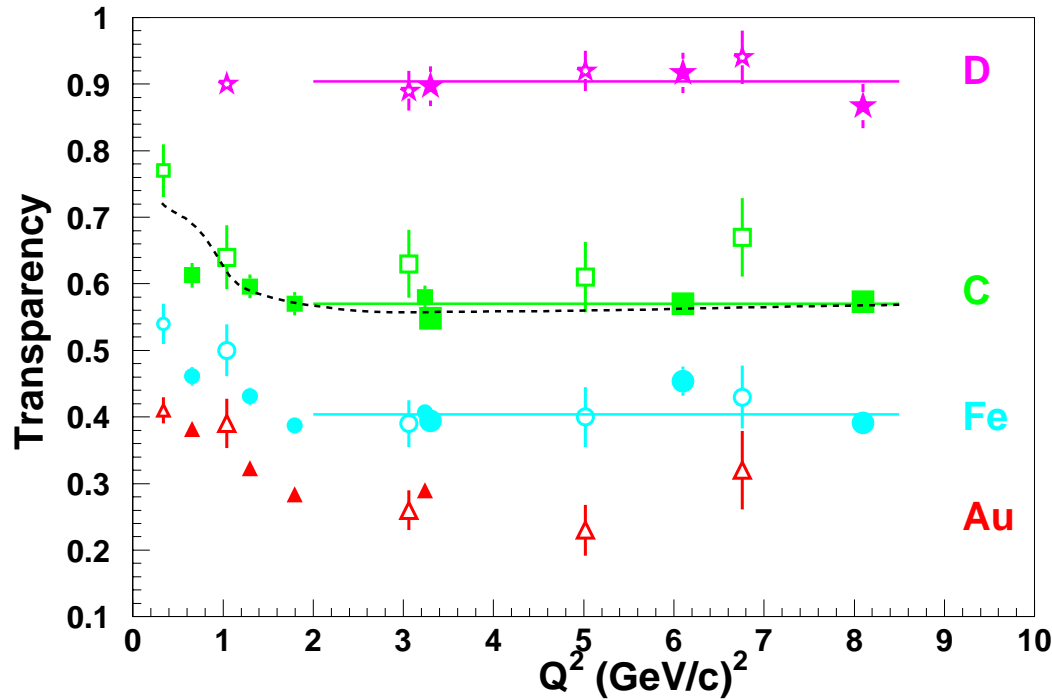
Ingredients

- σ_{hN} h-N cross-section
- Glauber multiple scattering approximation
(or better transport calculation!)
- Correlations & Final-State Interaction effects

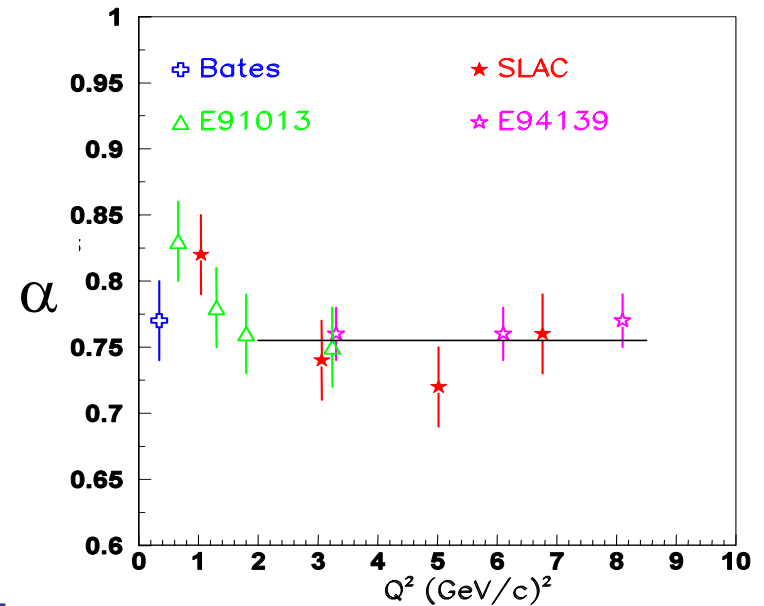
From fundamental considerations (quantum mechanics, relativity, nature of the strong interaction) it is predicted (Brodsky, Mueller) that **fast** protons scattered from the nucleus will have **decreased** final state interactions



Search for Color Transparency in Quasi-free $A(e, e'p)$ Scattering



Fit to $\sigma = \sigma_0 A^\alpha$



Constant value line fits give good description:

$$\chi^2/df = 1$$

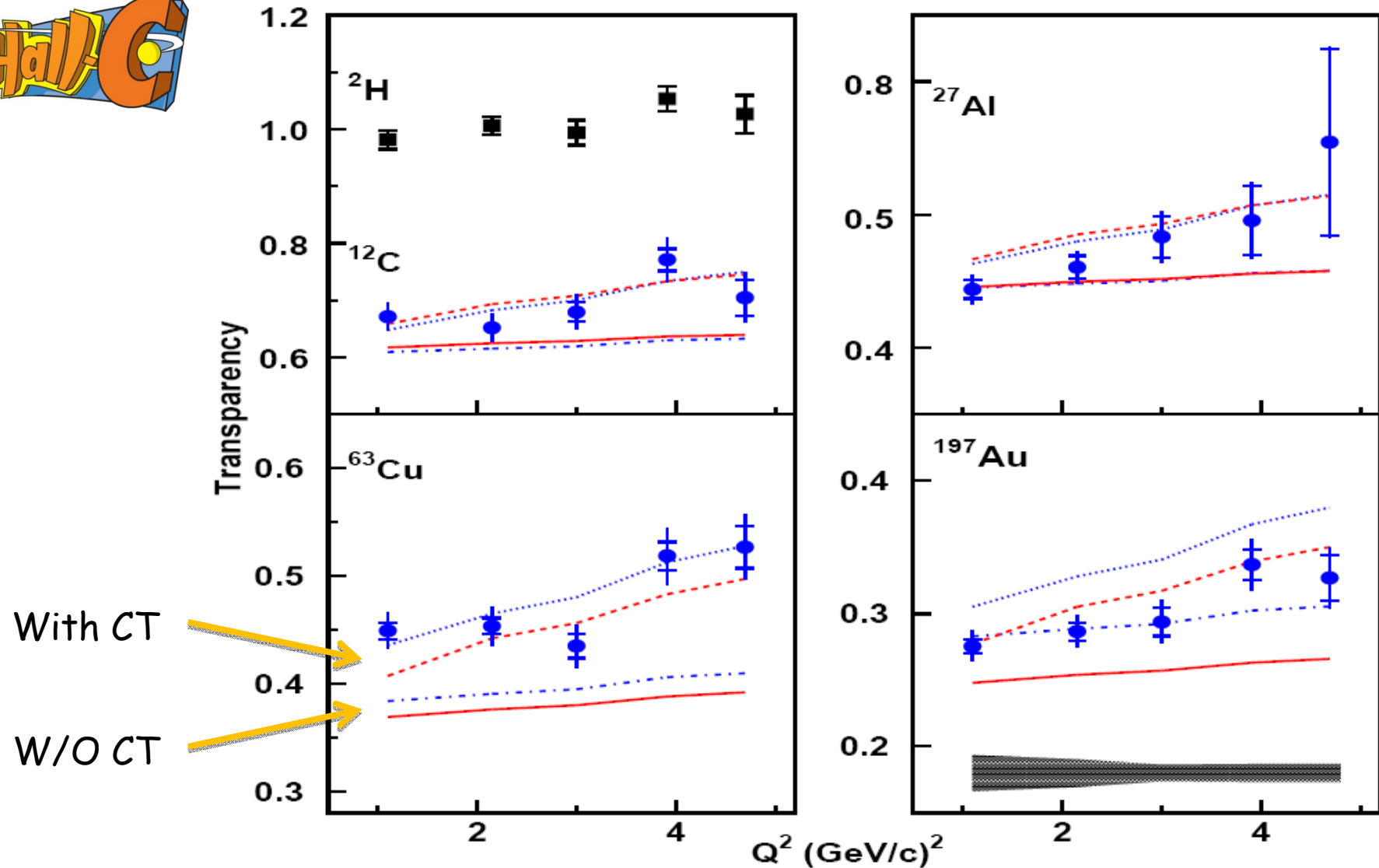
Conventional Nuclear Physics Calculation by Pandharipande *et al.* (1981) gives good description

$\alpha = \text{constant} = 0.75$

Close to proton-nucleus total cross section data!

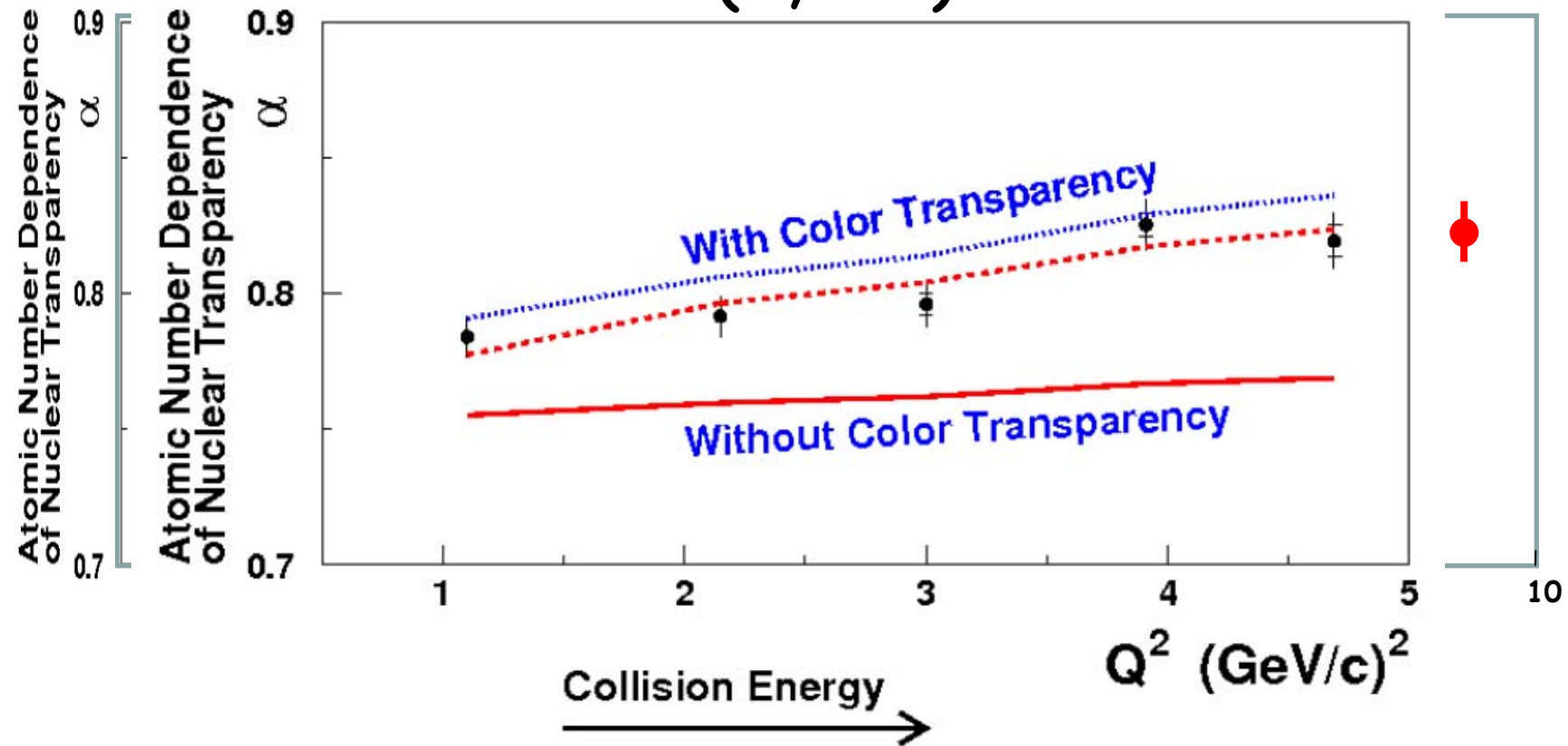
Physics of Nuclei: Color Transparency

$$A(e, e' \pi^+)$$



Physics of Nuclei: Color Transparency

$$A(e, e' \pi^+)$$



Total pion-nucleus cross section slowly disappears, or ...
pion escape probability increases → Color Transparency?
→ Unique possibility to map out at 12 GeV (up to $Q^2 = 10$)

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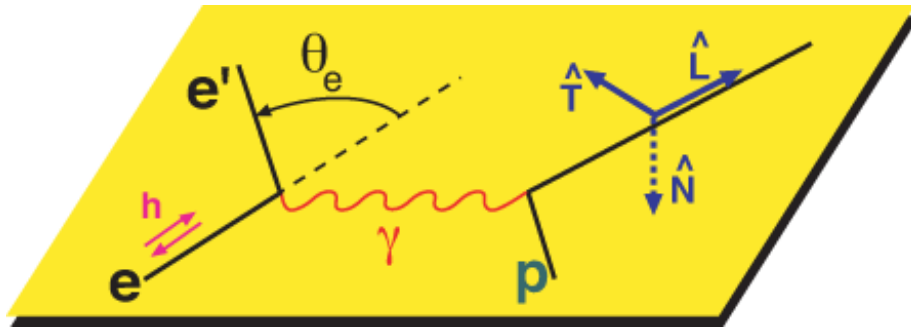
Charge and Magnetization in Nucleons and Pions

The Onset of the Parton Model

Revolutionized Polarized Beam Experiments!

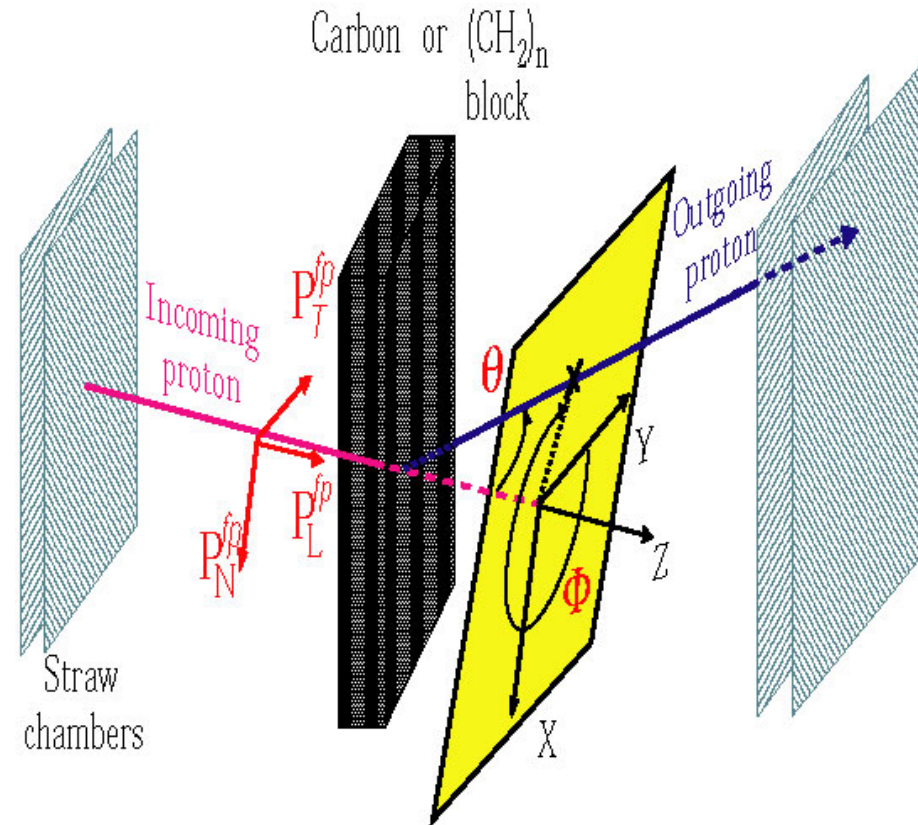
Precise access to (small) charge form factor of proton utilizing polarization transfer technique: $\vec{e} + p \rightarrow e' + \vec{p}$

Focal Plane Polarimeter



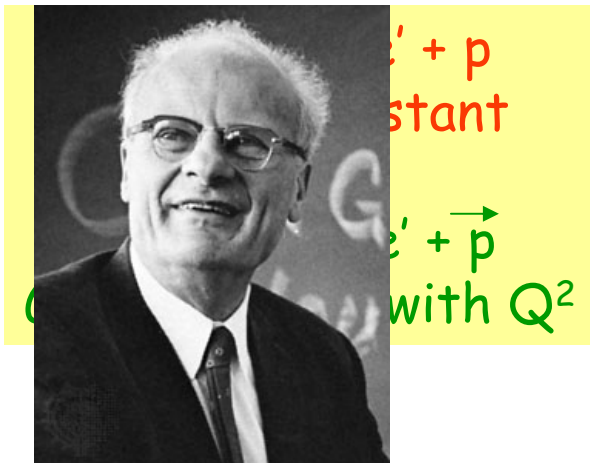
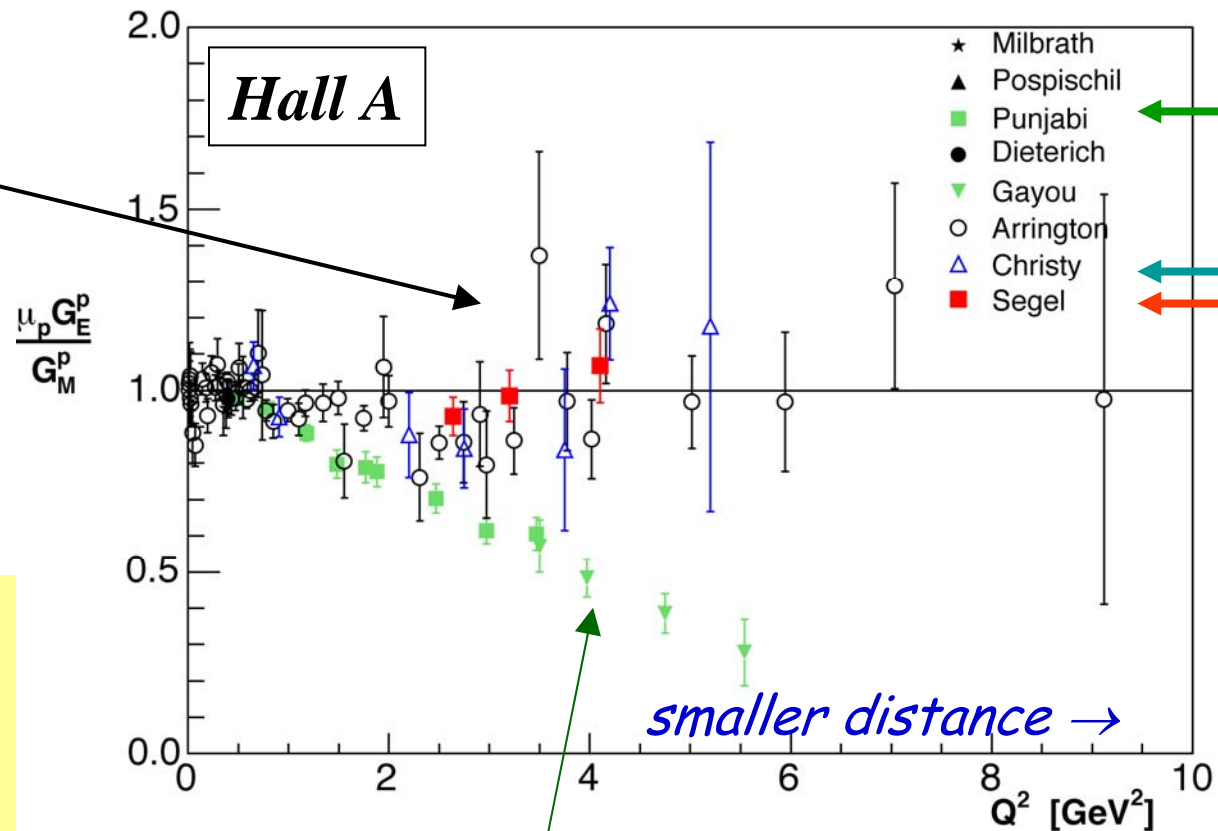
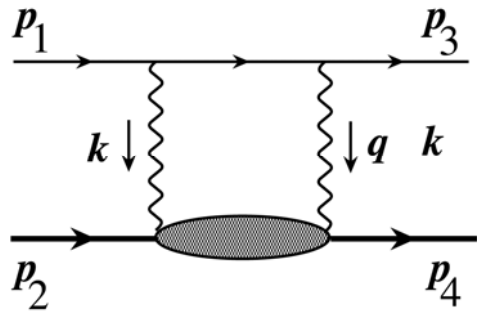
$$\frac{G_E}{G_M} = - \frac{P'_x}{P'_z} \frac{(E_i + E_f)}{2m} \tan \frac{\Theta_e}{2}$$

- No error contributions from
- analyzing power
 - beam polarimetry



Proton charge and magnetism in 2006

2- γ exchange important



H. Bethe
PR 72 (1947) 339
Lamb shift in hydrogen

charge depletion in interior of proton

Orbital motion of quarks play a key role
(Belitsky, Ji + Yuan PRL 91 (2003) 092003)

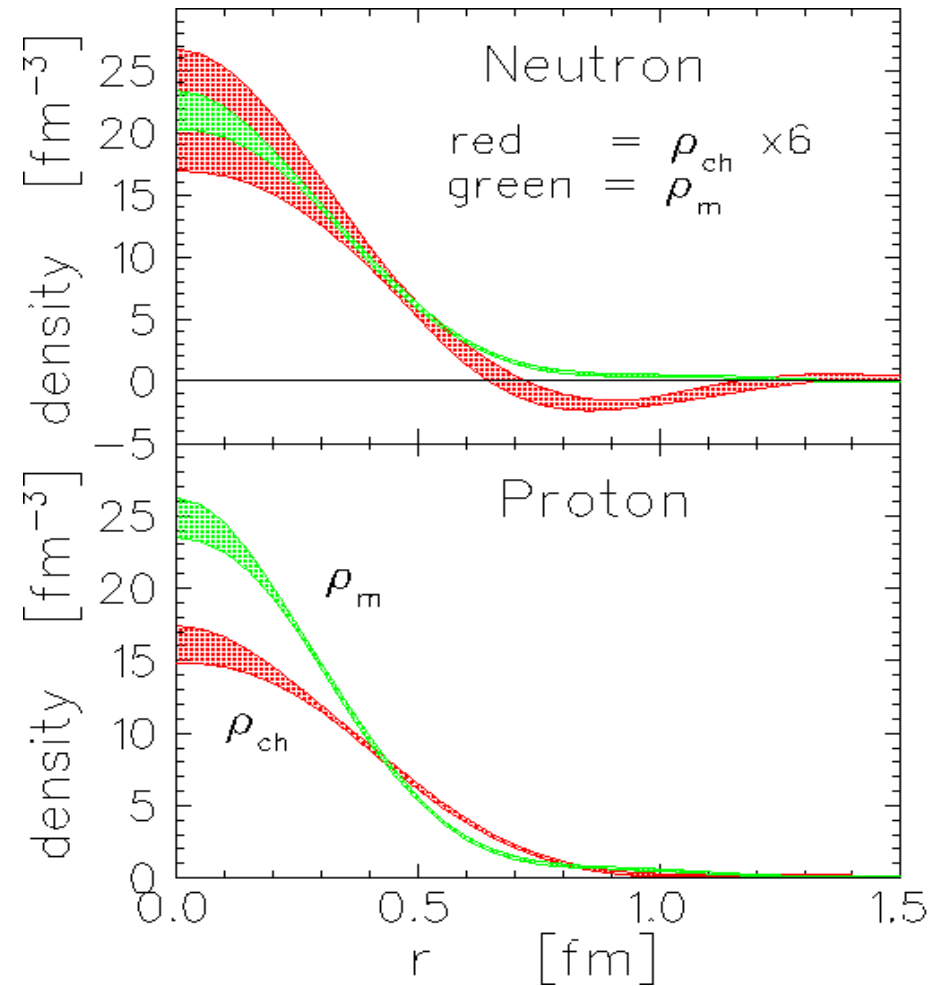
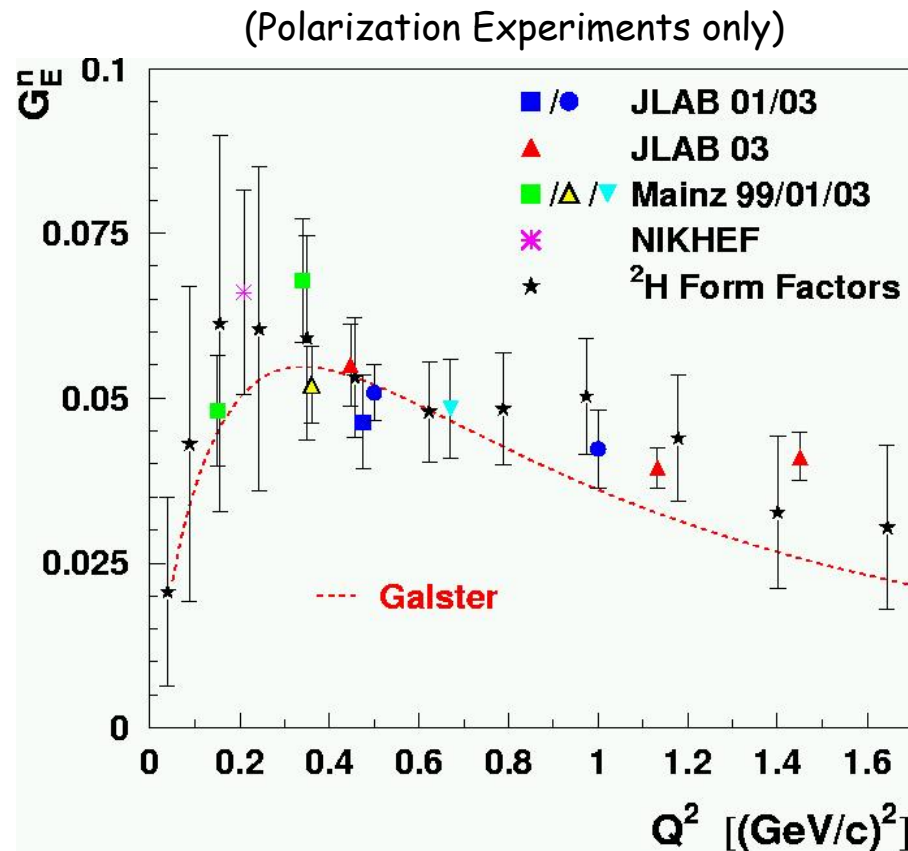
Hall A

What about the neutron?



Neutron has no charge, but does have a charge distributions: $n = p + \pi^-$, $n = ddu$.
 Use polarization and ${}^2\text{H}(e, e'n)$ to access.
"Guarantee" that electron hits a neutron AND electron transfers its polarization to this neutron.

charge and magnetization density



J. J. Kelly, PRC 66 (2002) 065203

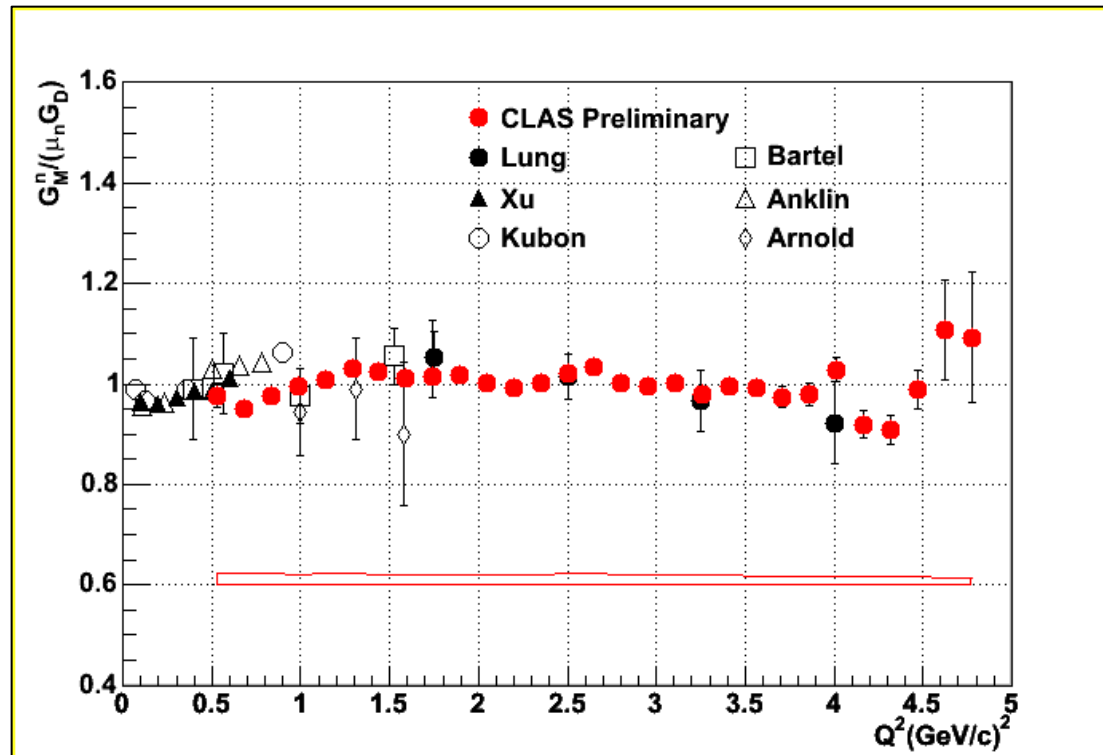
Hall B

Magnetic Form Factor of the Neutron

CLAS

- Use dual target (hydrogen & deuterium)
- Measure simultaneously $e^2\text{H} \rightarrow enX$ and $e^2\text{H} \rightarrow epX$, as well as $ep \rightarrow e\pi^+n$ for in-situ calibration of neutron detection efficiency in CLAS EC and TOF.

$$R_D = \frac{\frac{d\sigma}{d\Omega}[{}^2\text{H}(e, e'n)_{\text{QE}}]}{\frac{d\sigma}{d\Omega}[{}^2\text{H}(e, e'p)_{\text{QE}}]} = a \cdot R_{\text{free}}$$
$$= a \cdot \frac{\frac{(G_E^n)^2 + \tau(G_M^n)^2}{1+\tau} + 2\tau(G_M^n)^2 \tan^2(\frac{\theta}{2})}{\frac{(G_E^p)^2 + \tau(G_M^p)^2}{1+\tau} + 2\tau(G_M^p)^2 \tan^2(\frac{\theta}{2})}$$

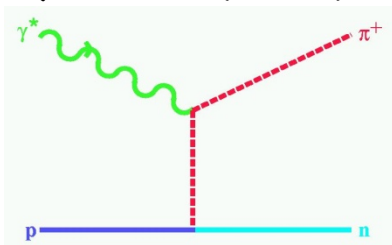


Pion's charge distribution



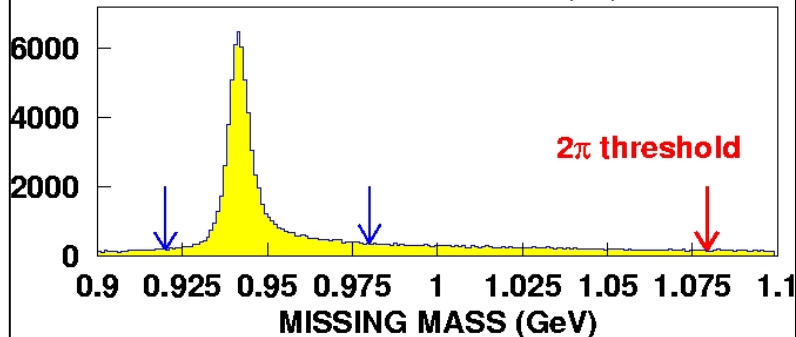
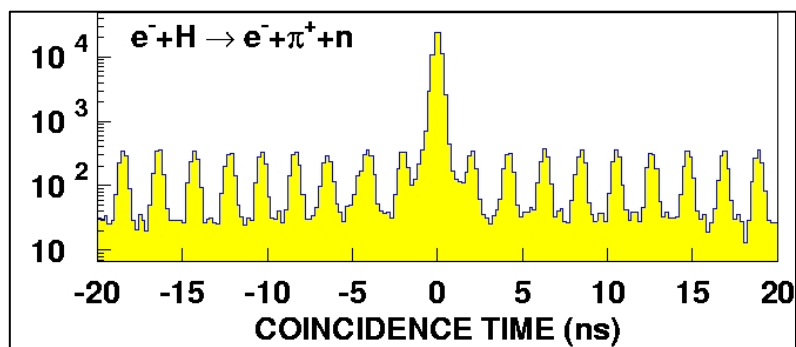
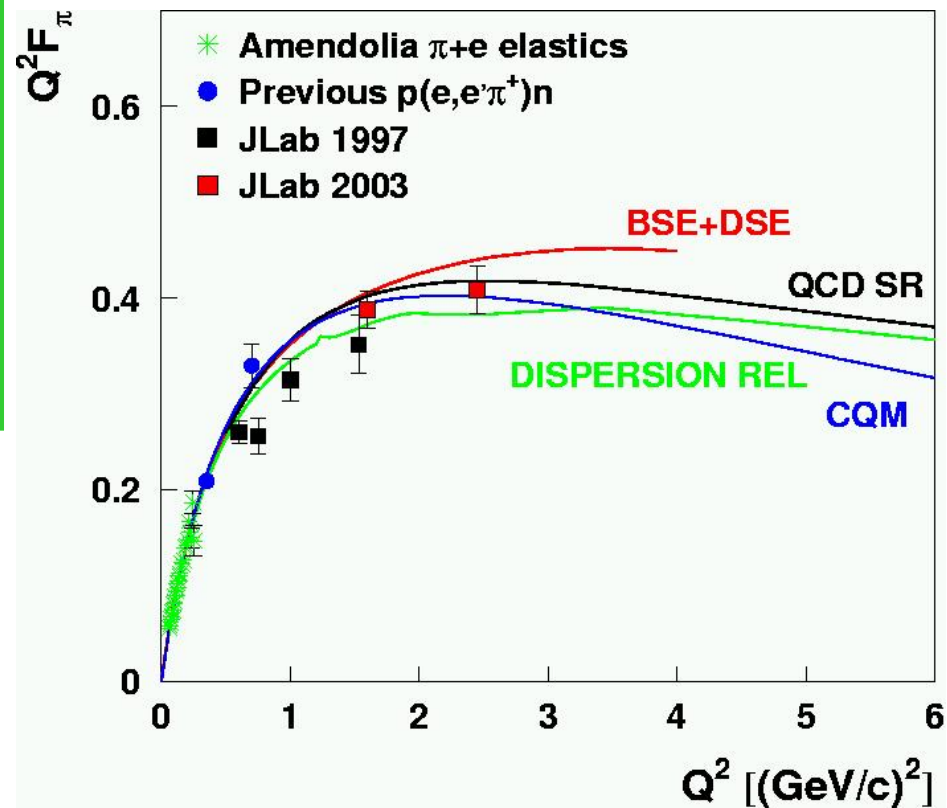
- At low Q^2 (< 0.3 $(\text{GeV}/c)^2$): use $\pi + e$ scattering $\rightarrow R_{\text{rms}} = 0.66$ fm

- At higher Q^2 : use $^1\text{H}(e, e'\pi^+)n$



- Use a realistic pion electroproduction (Regge-type) model to extract F_π

- In asymptotic region, $F_\pi \rightarrow 8\pi\alpha_s f_\pi^2 Q^{-2}$



T. Horn et al., nucl-ex/0607005
 V. Tadevosyan, et al., nucl-ex/0607007

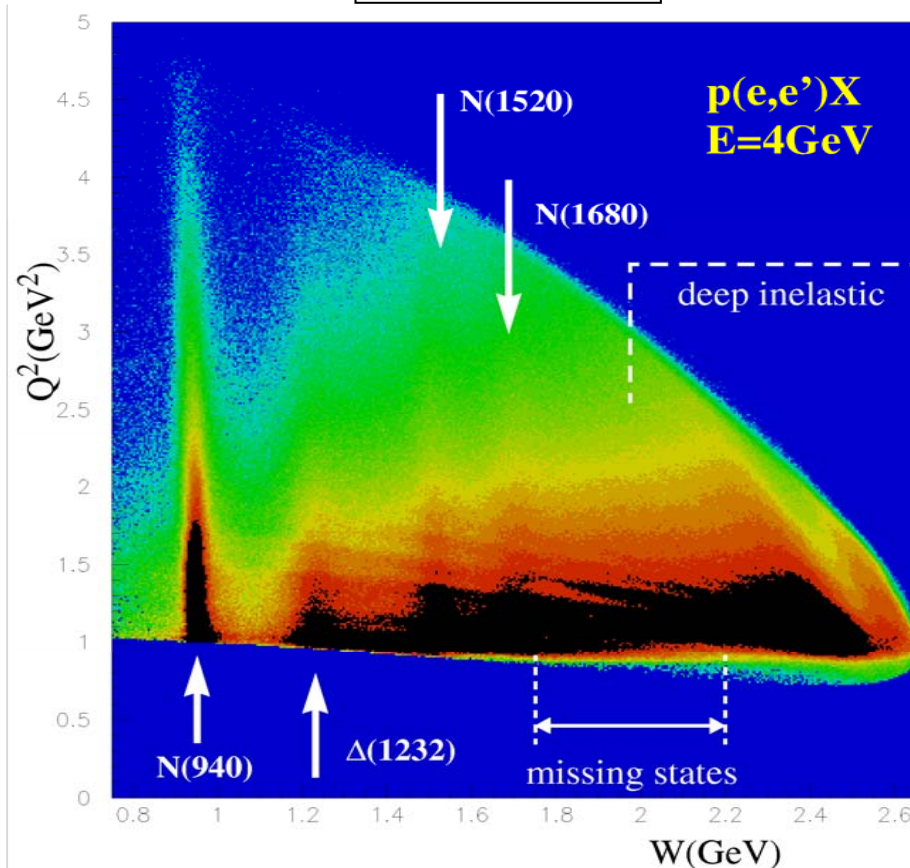
First measurements away from region where F_π is simply given by the π radius

Hall B

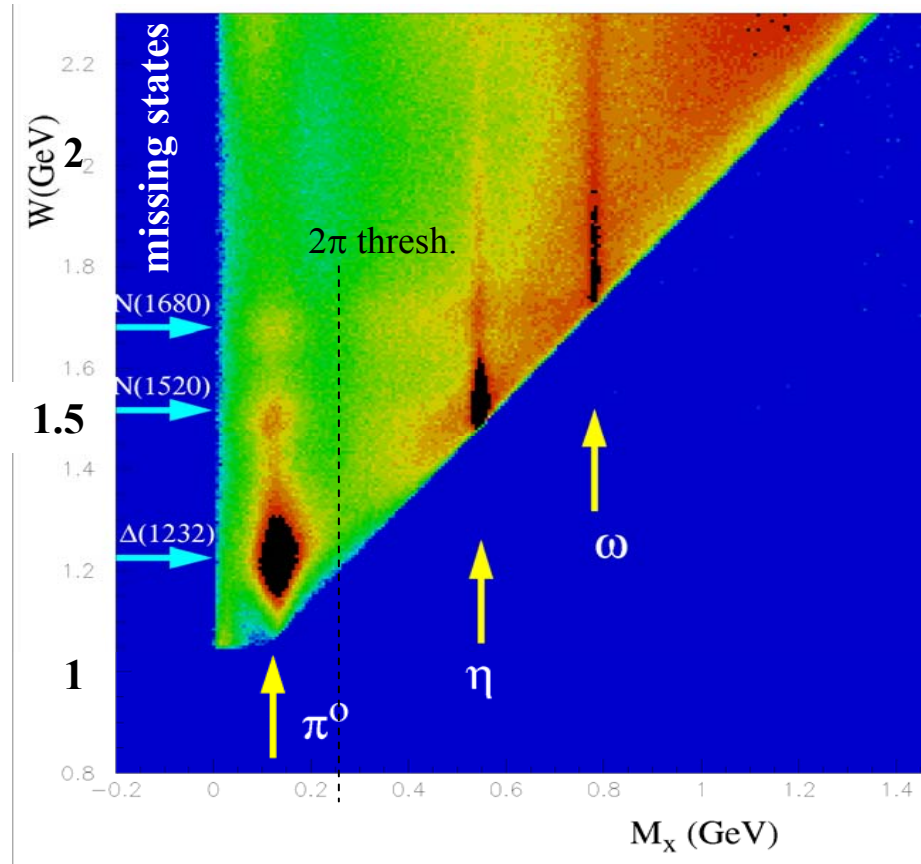
Electron Scattering

CLAS

$p(e,e')X$

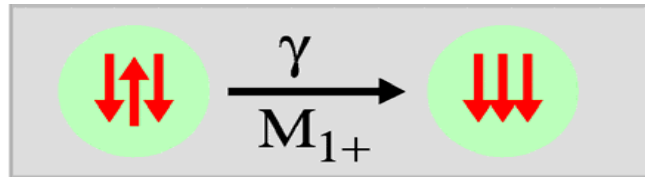


$p(e,e'p)X$

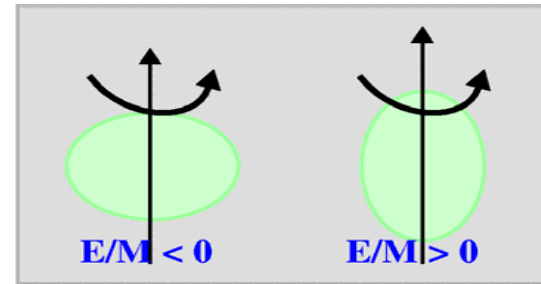


➤ Resonances cannot be uniquely separated in inclusive scattering → measure exclusive processes.

The $\gamma N \Delta(1232)$ Quadrupole Transition

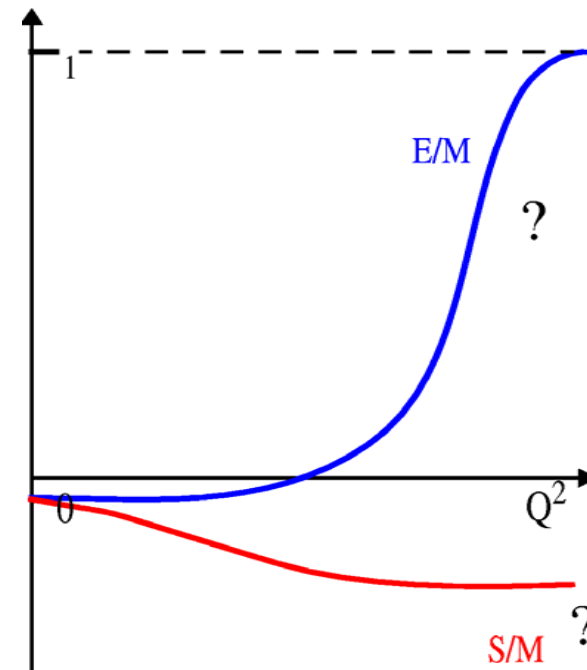


SU(6): $E_{1+} = S_{1+} = 0$



(A. Buchmann, E. Henley, 2000)

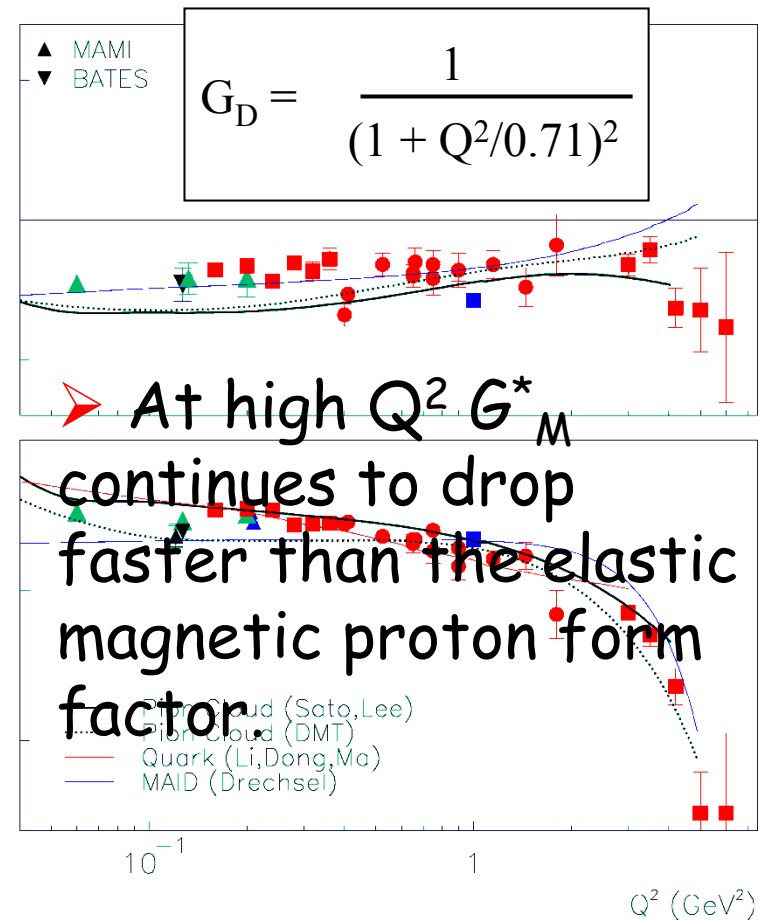
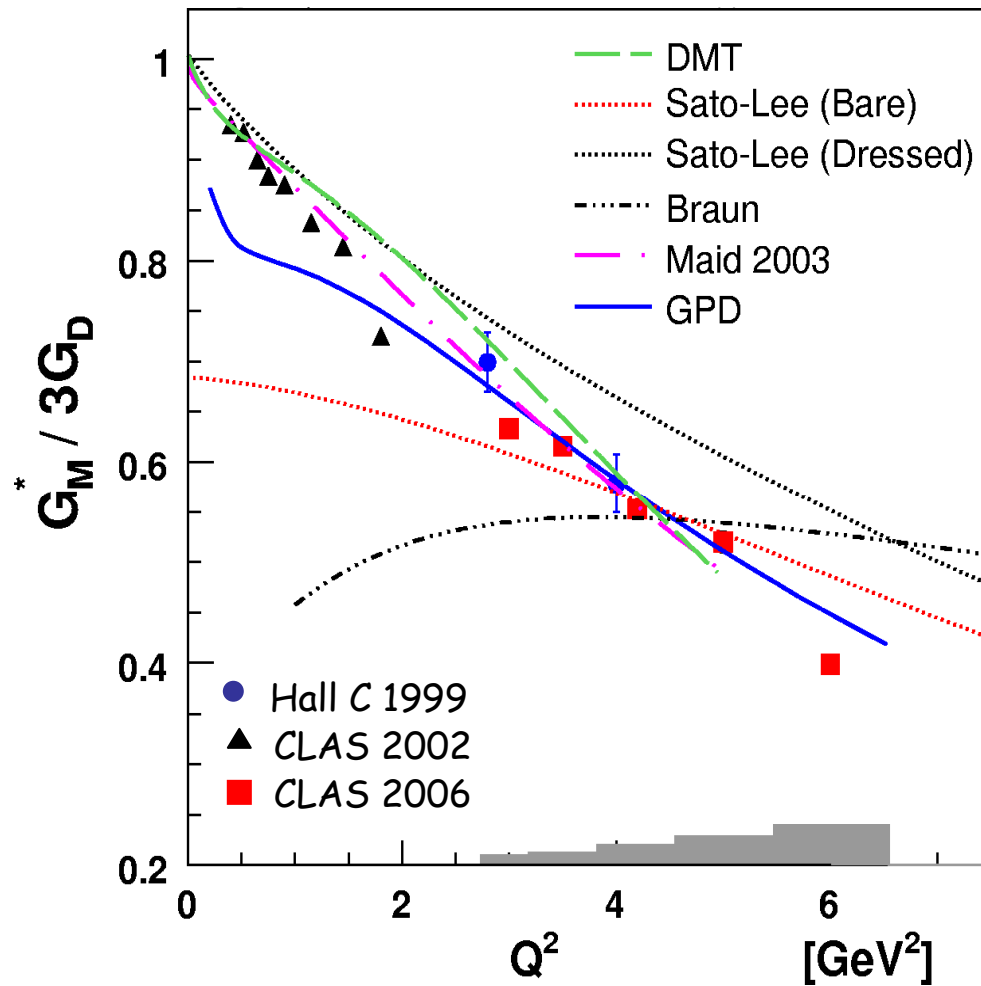
		E/M	S/M
	pion cloud	~0.03	~0.1
	one-gluon exch.	~ 0.01	
	pQCD	+1	const.



Hall B

Transition amplitudes $\gamma_{\nu p} \rightarrow N_{3/2^+} (1232)$
(The $N\text{-}\Delta$ Transition)

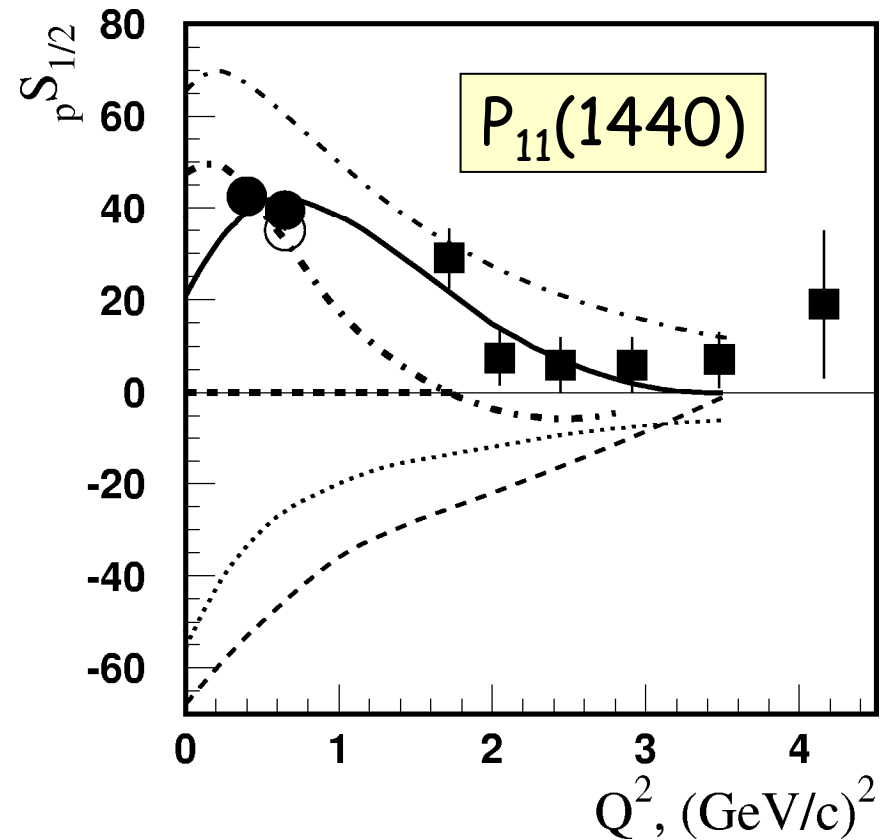
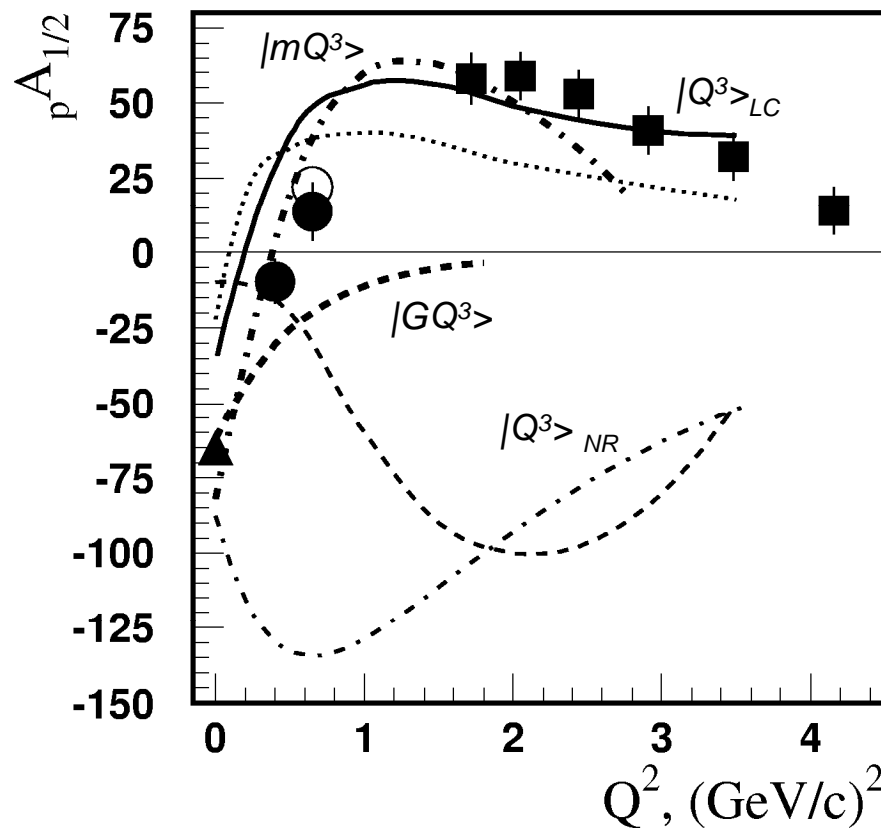
CLAS



Hall B

Transition amplitudes $\gamma_{\nu p} \rightarrow N_{1/2^+}(1440)$
(The Elusive Roper Resonance)

CLAS



At large distances the Roper resonance shows behavior similar to what is predicted in a model containing large meson contributions, at short distances the data are consistent with behavior expected from a constituent quark picture.

The proton's magnetic moment



Nobel Prize, 1943: "for his contribution to the development of the molecular ray method and his discovery of the magnetic moment of the proton"

$$\mu_p = 2.5 \text{ nuclear magnetons, } \pm 10\% \quad (1933)$$

Otto Stern

2002 experiment:

$$\mu_p = 2.792847351(28) \mu_N$$

$$\mu_n = -1.91304274(45) \mu_N$$

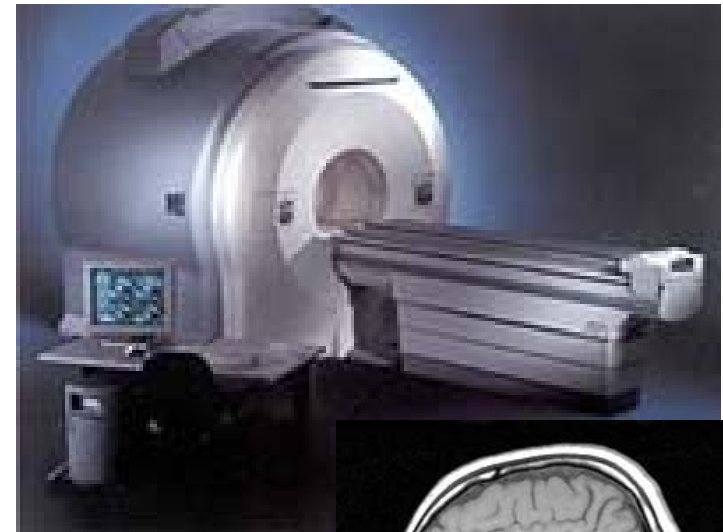
2006 theory:

$$\mu_p \sim 2.8 \mu_N$$

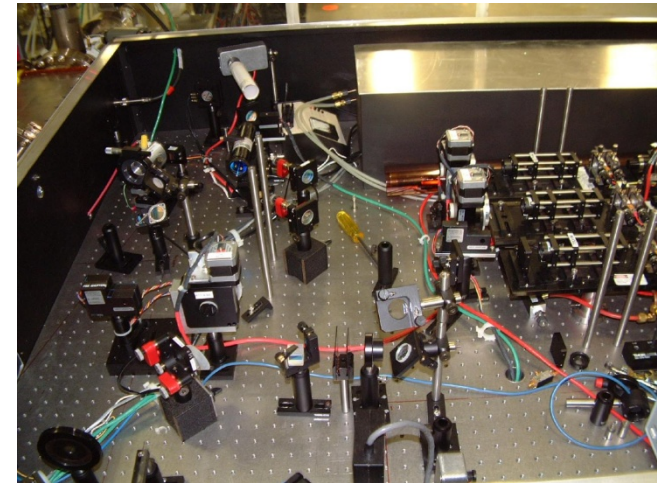
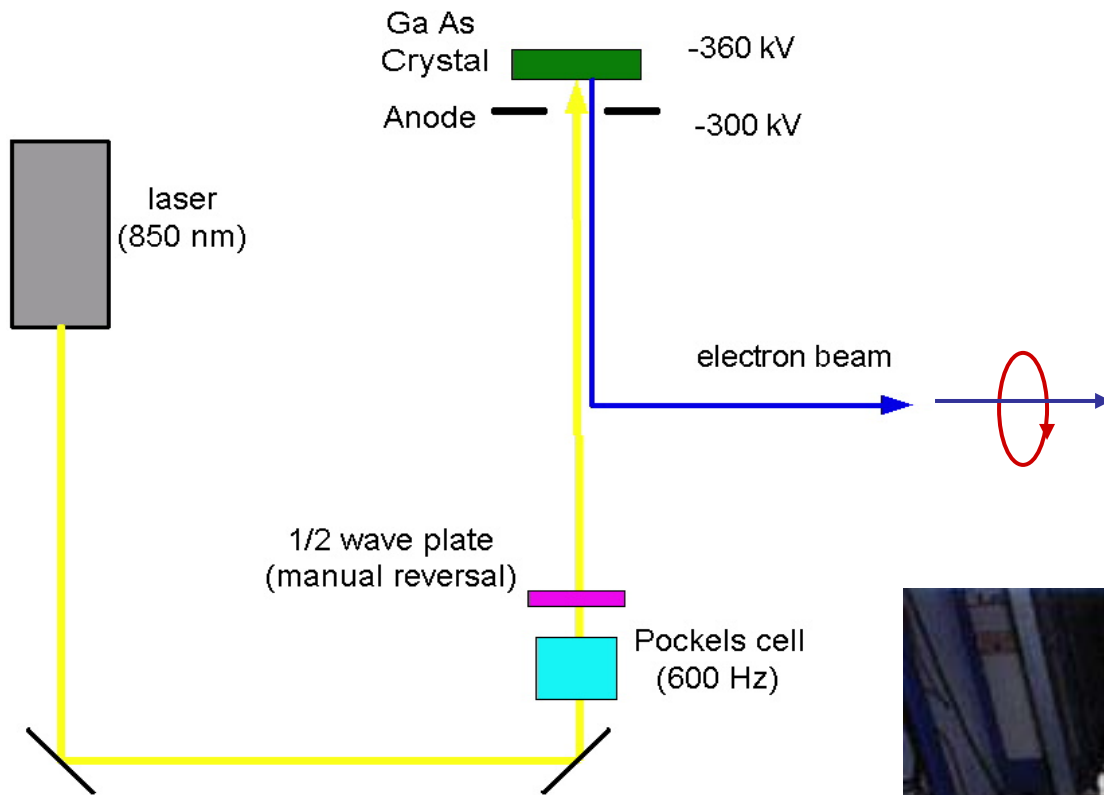
$$\mu_n \sim -1.8 \mu_N$$

How do the quark contributions add up?

How are charge and magnetism distributed?



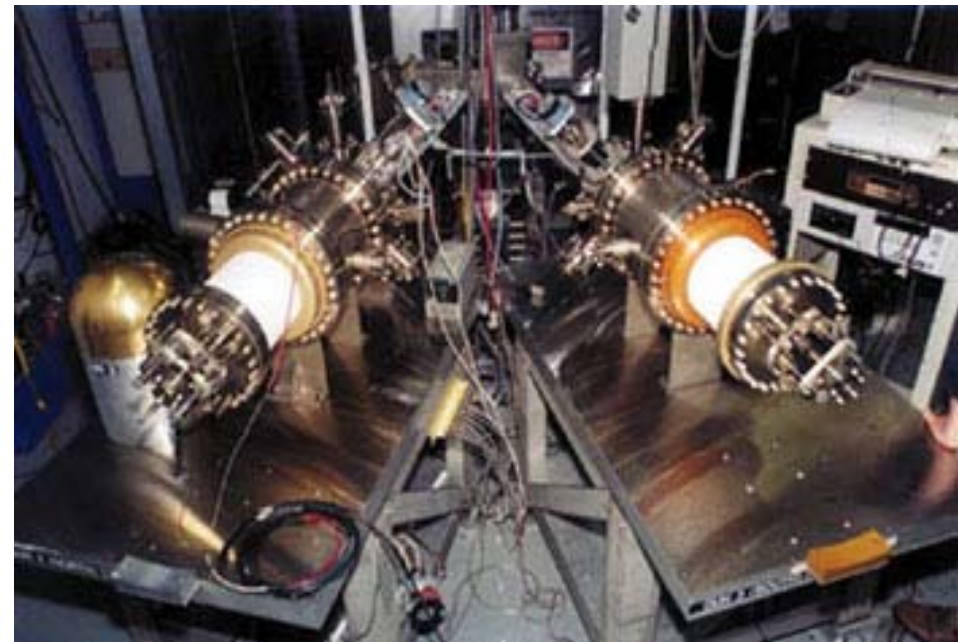
JLab: Polarized Electrons!!!



Electron retains circular polarization of laser beam

Reverse polarization of beam at rate of 30 Hz

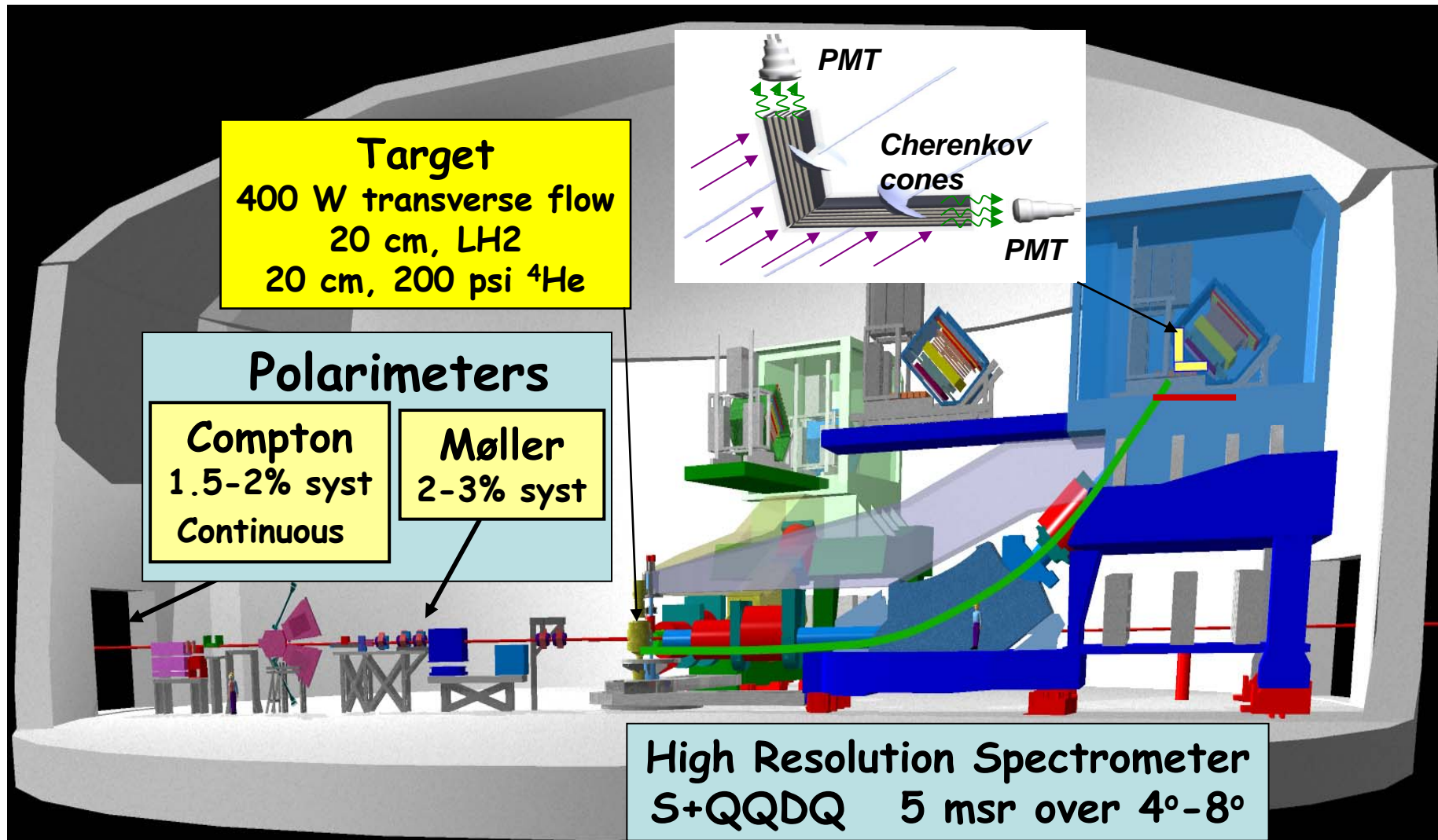
Feedback on laser intensity and position at high rate



Hall A

Parity Violating Studies on ^1H and ^4He

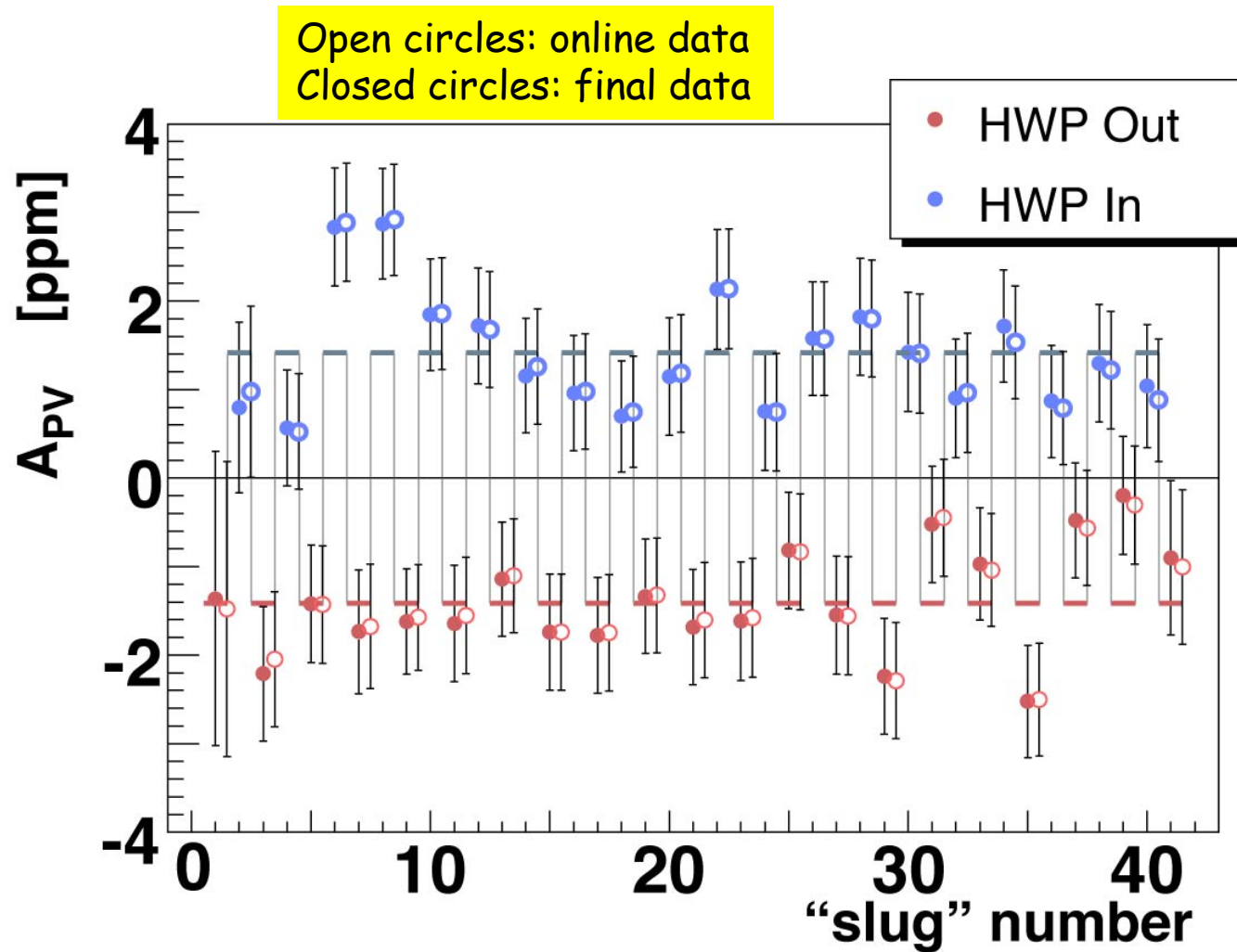
The HAPPEX Program: Strange Quark Contributions to the Proton



Hall A

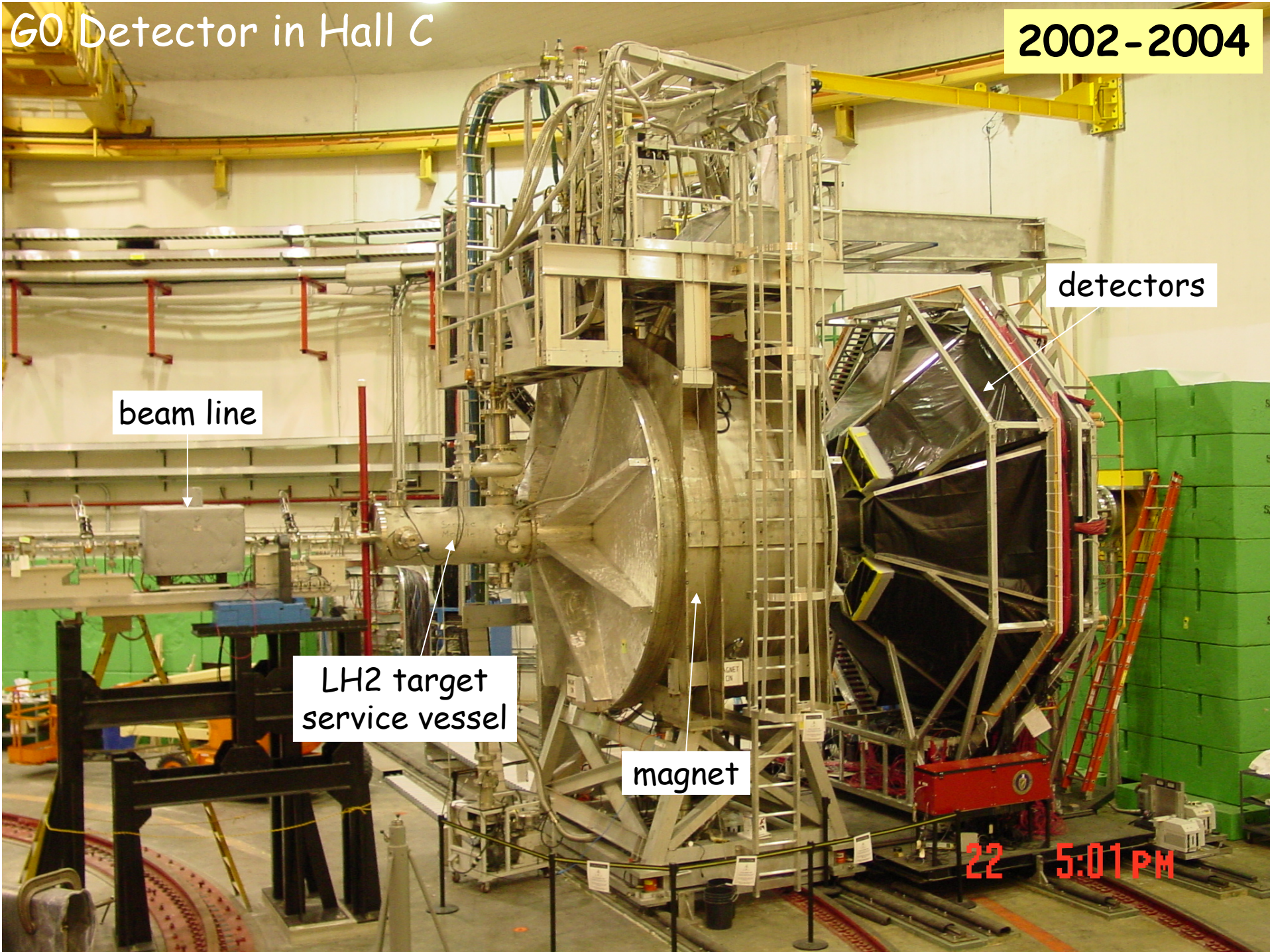
Parity Violating Studies on ^1H and ^4He

The HAPPEX Program: Strange Quark Contributions to the Proton



GO Detector in Hall C

2002-2004



beam line

LH2 target service vessel

magnet

detectors

22 5:01 PM

(Rotated) G0 Detector in Hall C

2006-2007

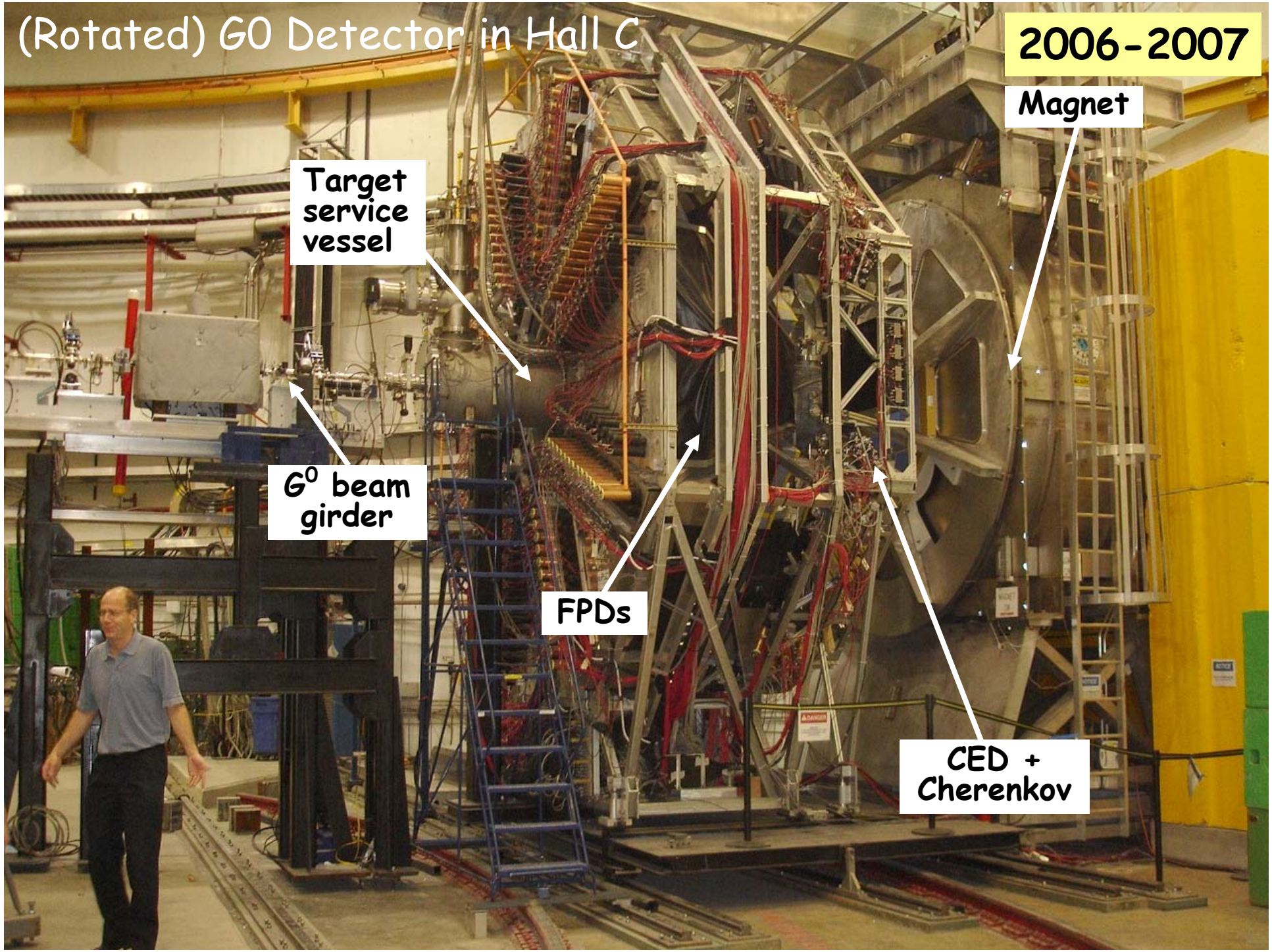
Magnet

Target service vessel

G⁰ beam girder

FPDs

CED + Cherenkov





JLab polarized beam



GO forward running beam:

- strained GaAs ($P_B \sim 73\%$)
- 32 ns pulse spacing
- 40 μA beam current

HAPPEX-II beam (2005):

- superlattice ($P_B > 85\%$)
- 2 ns pulse spacing
- 35 μA beam current

Beam Parameter	GO beam (Hall C)	HAPPEX beam (Hall A)
Charge asymmetry	-0.14 ± 0.32 ppm	-2.6 ± 0.15 ppm
Position difference	4 ± 4 nm	-8 ± 3 nm
angle difference	1.5 ± 1 nrad	4 ± 2 nrad
Energy difference	29 ± 4 eV	66 ± 3 eV
Total correction to Asymmetry	-0.02 ± 0.01 ppm	0.08 ± 0.03 ppm

The spatial distribution of quarks and the proton's magnetism

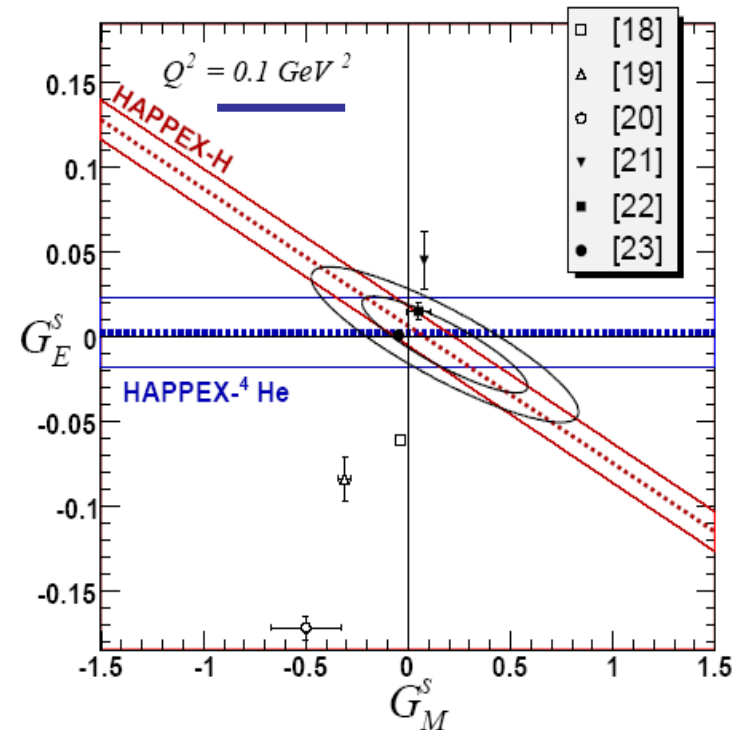
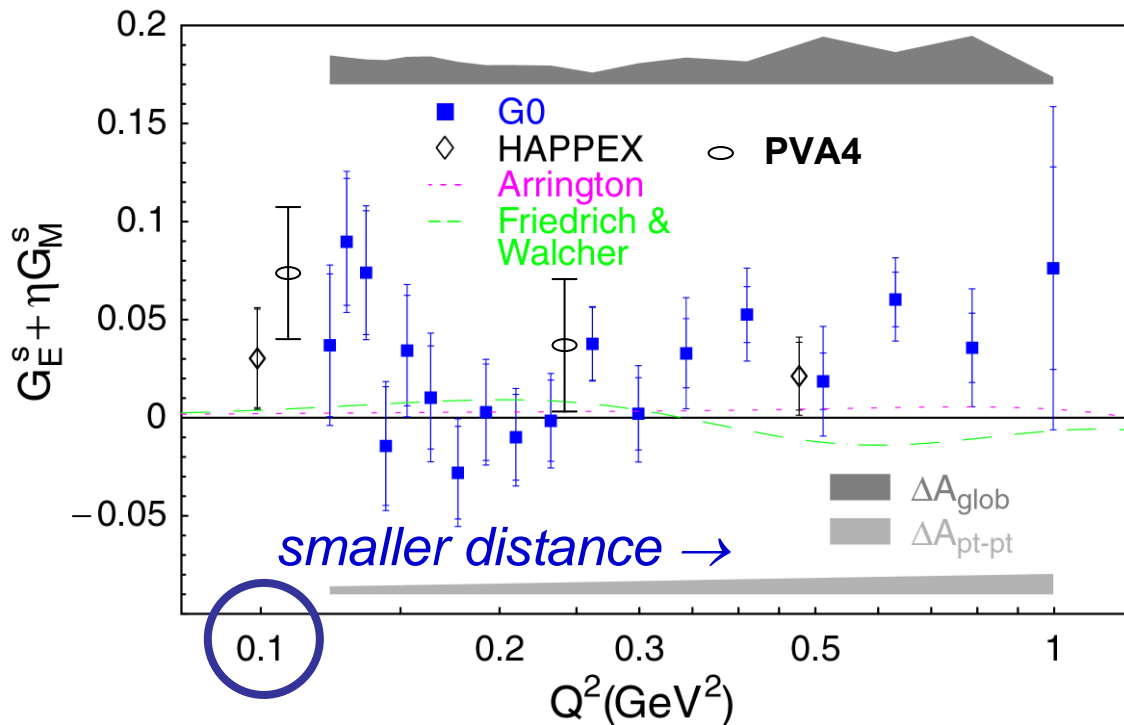


Hall A

$$G_M^p(Q^2) = \frac{2}{3} G_M^u(Q^2) - \frac{1}{3} G_M^d(Q^2) - \frac{1}{3} G_M^s(Q^2)$$

proton charge/magnetism
 neutron charge/magnetism
 proton response to Weak force

up
 down
 strange ← ~ 5%



Extracting Nucleon Strange Form Factors from World Data

Ross Young (JLab-Theory), Julie Roche, Roger Carlini (JLab), Tony Thomas (JLab-Theory)

Approach: Use the complete (SAMPLE, PVA4, HAPPEX, G0) world set of parity-violating electron scattering asymmetries up to $Q^2 = 0.3 \text{ GeV}^2$.

$$G_E^s = \rho_s Q^2 + \rho'_s Q^4$$
$$G_M^s = \mu_s + \mu'_s Q^2$$

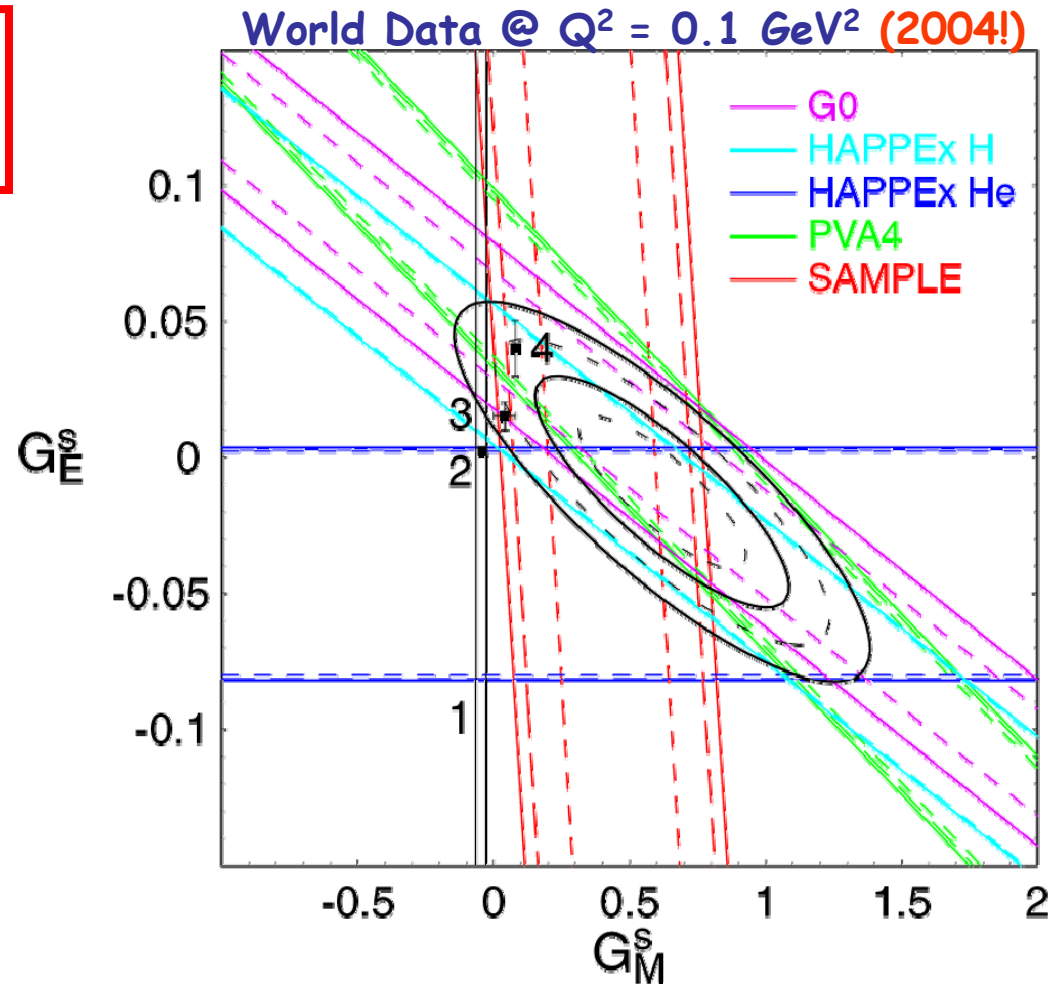
Contours

1 σ , 2 σ

68.3, 95.5% CL

Theories

1. Leinweber, et al.
PRL **94** (05) 212001
2. Lyubovitskij, et al.
PRC **66** (02) 055204
3. Lewis, et al.
PRD **67** (03) 013003
4. Silva, et al.
PRD **65** (01) 014016



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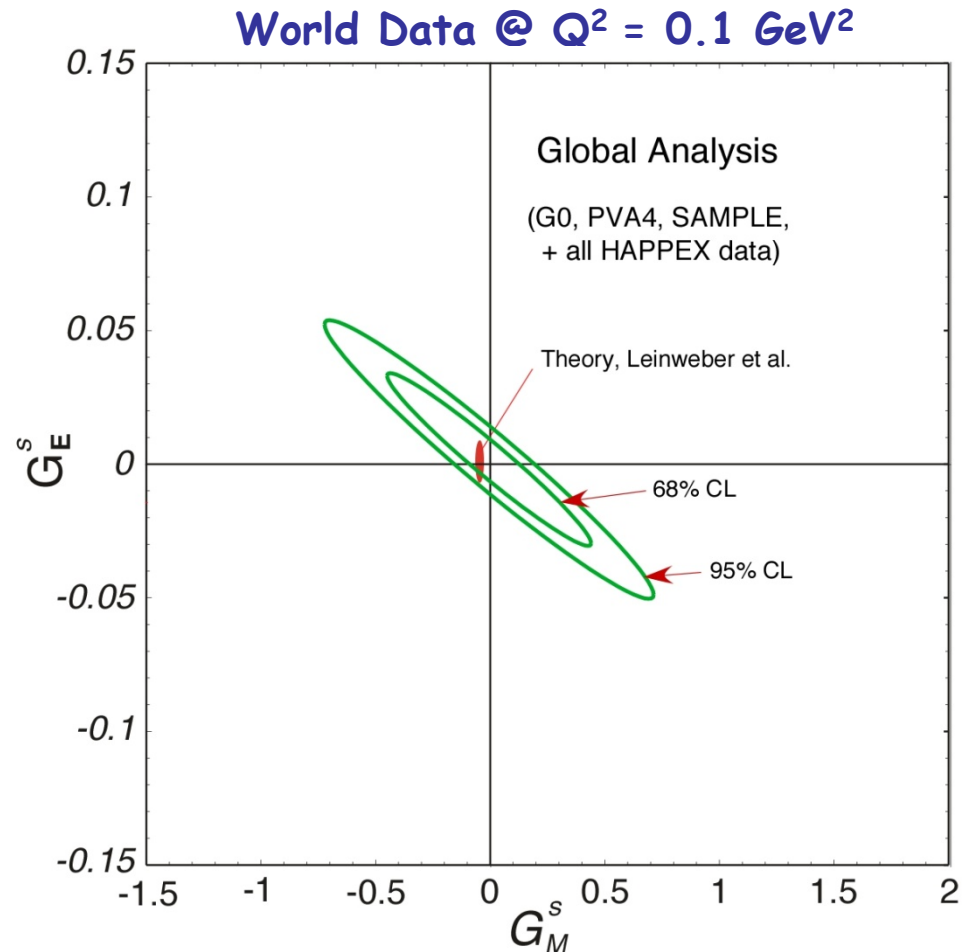
Contours

$1\sigma, 2\sigma$
68.3, 95.5% CL

Theory

Leinweber, et al.
PRL **94** (05) 212001;
hep-lat/0601025

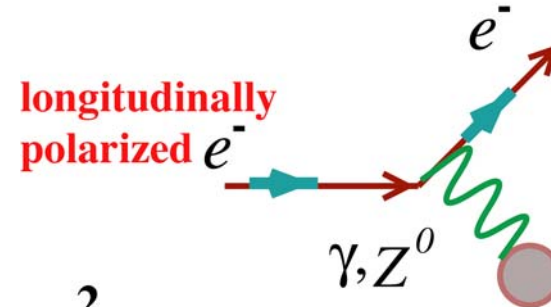
... or include recent
HAPPEX-H and -He data



PV Asymmetries

Weak Neutral Current (WNC) Interactions at $Q^2 \ll M_Z^2$

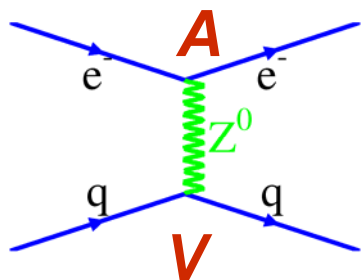
Longitudinally Polarized
Electron Scattering off
Unpolarized Fixed Targets



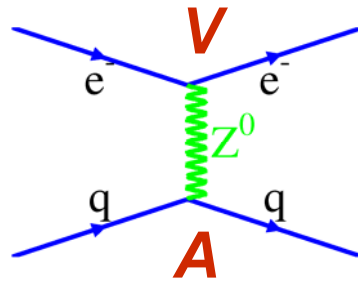
$$\sigma \propto |A_\gamma + A_{\text{weak}}|^2$$

$$-A_{\text{LR}} = A_{\text{PV}} = \frac{\sigma_{\uparrow} - \sigma_{\downarrow}}{\sigma_{\uparrow} + \sigma_{\downarrow}} \sim \frac{A_{\text{weak}}}{A_\gamma} \sim \frac{G_F Q^2}{4\pi\alpha} (g_A^e g_V^T + \beta g_V^e g_A^T)$$

Electron-Quark Phenomenology



$$C_{1i} \equiv 2g_A^e g_V^i$$

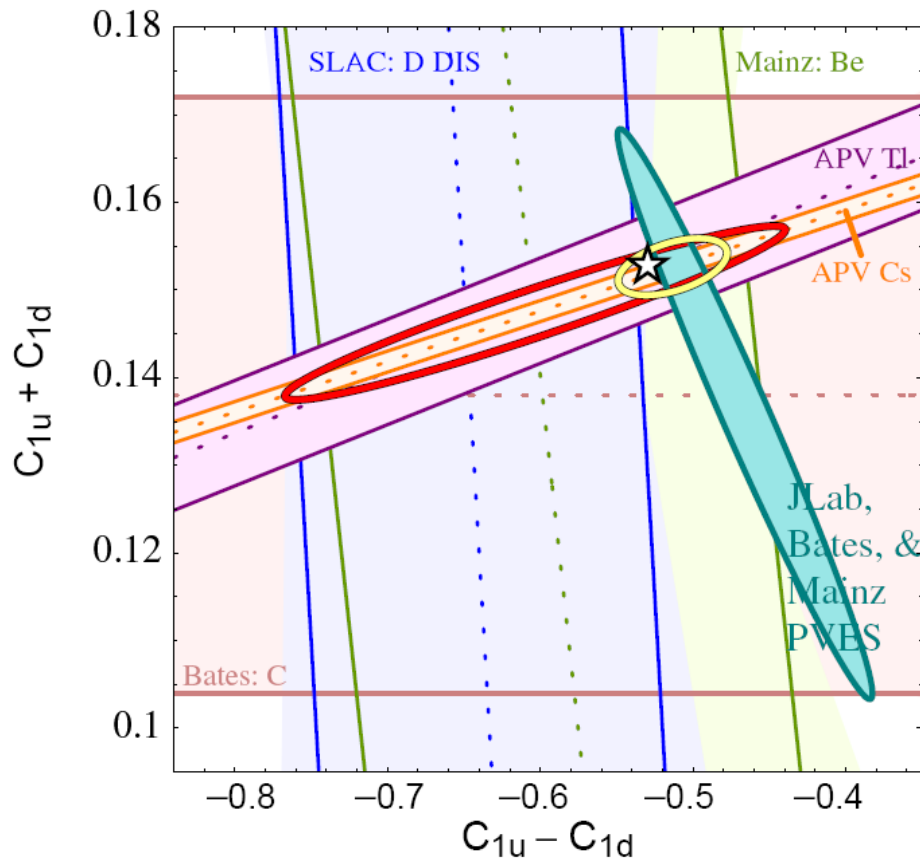


$$C_{2i} \equiv 2g_V^e g_A^i$$

$$\begin{aligned} C_{1u} &= -\frac{1}{2} + \frac{4}{3} \sin^2(\theta_W) \approx -0.19 \\ C_{1d} &= \frac{1}{2} - \frac{2}{3} \sin^2(\theta_W) \approx 0.35 \\ C_{2u} &= -\frac{1}{2} + 2 \sin^2(\theta_W) \approx -0.04 \\ C_{2d} &= \frac{1}{2} - 2 \sin^2(\theta_W) \approx 0.04. \end{aligned}$$

Use precision data to get new update on C_{1q} couplings...

→ Dramatic improvement in knowledge of weak couplings!



Factor of 5 increase in precision of Standard Model test

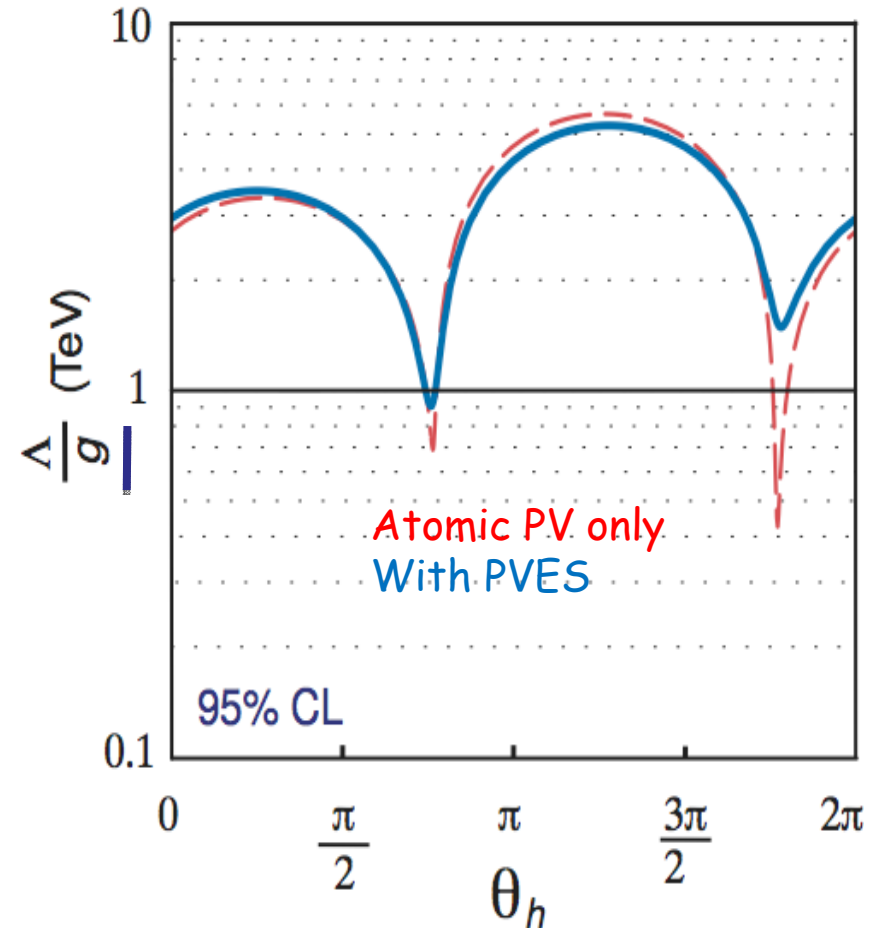
$$\mathcal{L}_{\text{SM}}^{\text{PV}} = -\frac{G_F}{\sqrt{2}} \bar{e} \gamma_\mu \gamma_5 e \sum_q C_{1q}^{\text{SM}} \bar{q} \gamma^\mu q$$

Erlar et al., PR D68 (2003)

$$\mathcal{L}_{\text{NP}}^{\text{PV}} = \frac{g^2}{4\Lambda^2} \bar{e} \gamma_\mu \gamma_5 e \sum_q h_V^q \bar{q} \gamma^\mu q$$

Full isospin coverage for limits on new physics!

$$h_V^u = \cos \theta_h \quad h_V^d = \sin \theta_h$$

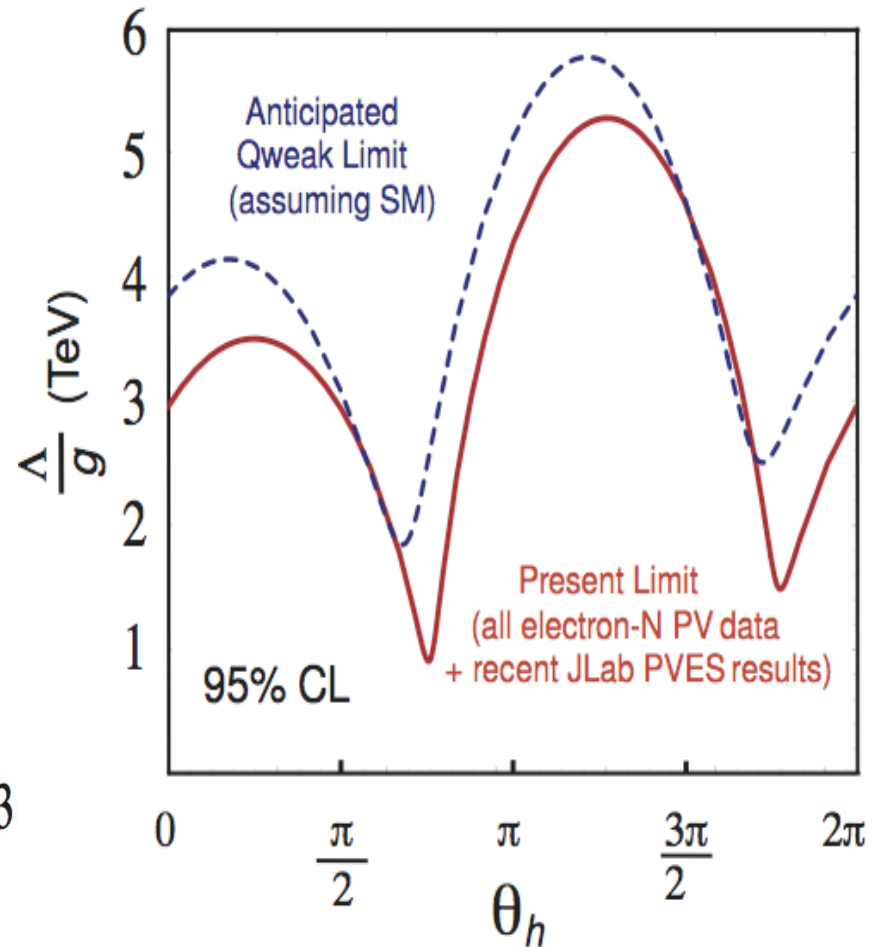
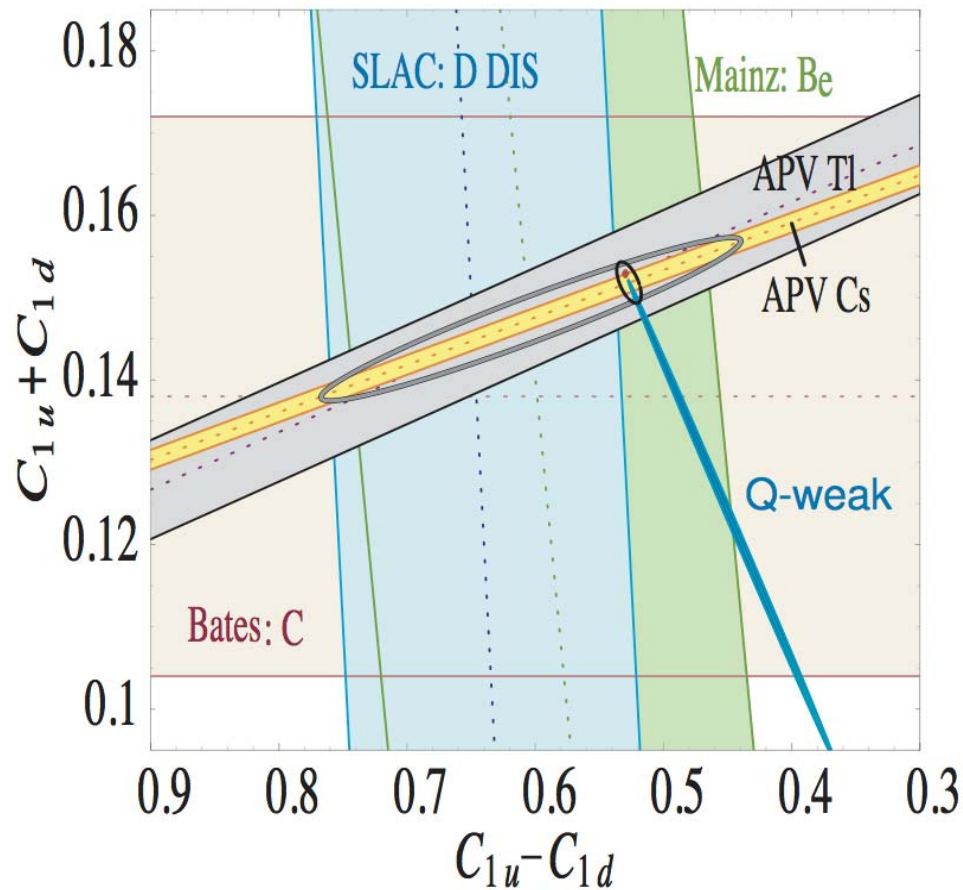


New Physics Scale > 0.9 TeV

Possible Impact of Qweak Experiment (2010-2012)



Qweak constrains new physics to beyond 2 TeV



CEBAF's Original Mission Statement

Key Mission and Principal Focus (1987):

The study of the largely unexplored transition between the nucleon-meson and the quark-gluon descriptions of nuclear matter.

The Role of Quarks in Nuclear Physics

Related Areas of Study:

- Do individual nucleons change their size, shape, and quark structure in the nuclear medium?
- How do nucleons cluster in the nuclear medium?

Pushing the Limits of the Standard Model of Nuclear Physics

- **What are the properties of the force which binds quarks into nucleons and nuclei at distances where this force is strong and the quark confinement mechanism is important?**

Charge and Magnetization in Nucleons and Pions

The Onset of the Parton Model

The Double-Faced Strong Force

Confinement
Nucleons

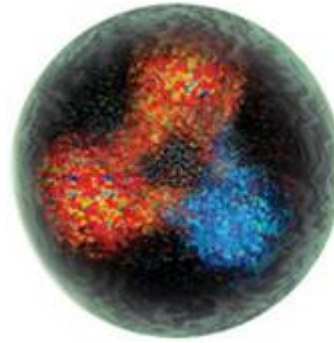
$$Q < \Lambda$$

$$\alpha_s(Q) > 1$$

Constituent
Quarks

$$Q > \Lambda$$

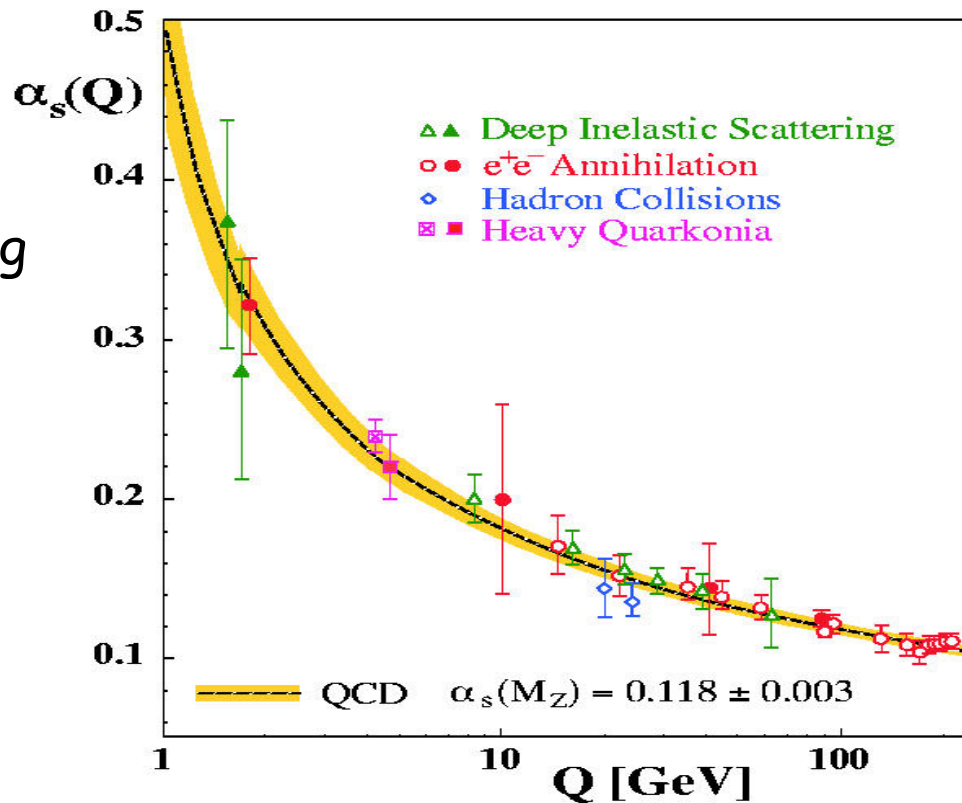
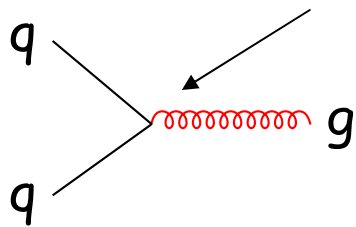
$$\alpha_s(Q) \text{ large}$$



Asymptotically
Free Quarks

$$Q \gg \Lambda$$

$$\alpha_s(Q) \text{ small}$$



One parameter, Λ_{QCD} ,
~ Mass Scale or
Inverse Distance Scale
where $\alpha_s(Q) = \infty$

"Separates" Confinement
and Perturbative Regions

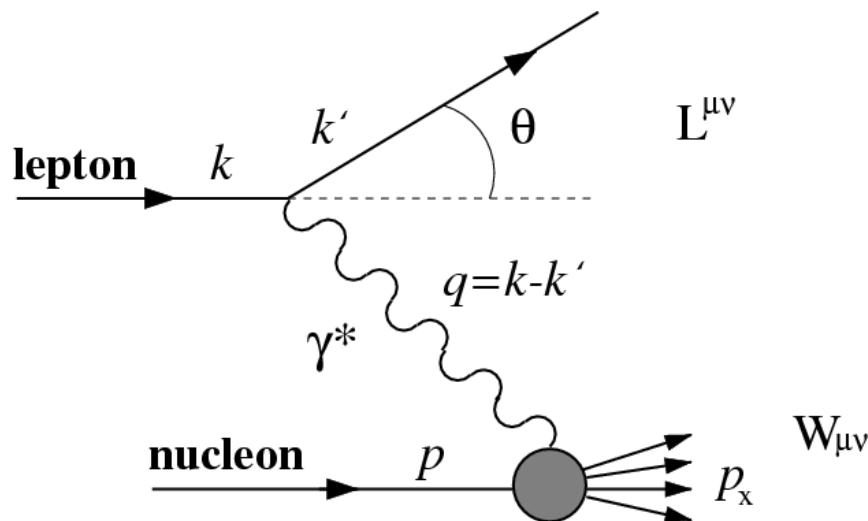
Mass and Radius of the
Proton are (almost)
completely governed by

$$\Lambda_{\text{QCD}} \approx 0.213 \text{ GeV}$$

Quark Model

Quark Parton Model

Inclusive $^1\text{H}(e, e')$ Scattering - Formalism



Cross section for inclusive lepton (electron) scattering:

$$\frac{d\sigma}{d\Omega dE'} = \frac{\alpha^2}{Q^4} \frac{E}{E'} L_{\mu\nu} W^{\mu\nu}$$

In terms of virtual photon polarization ε :

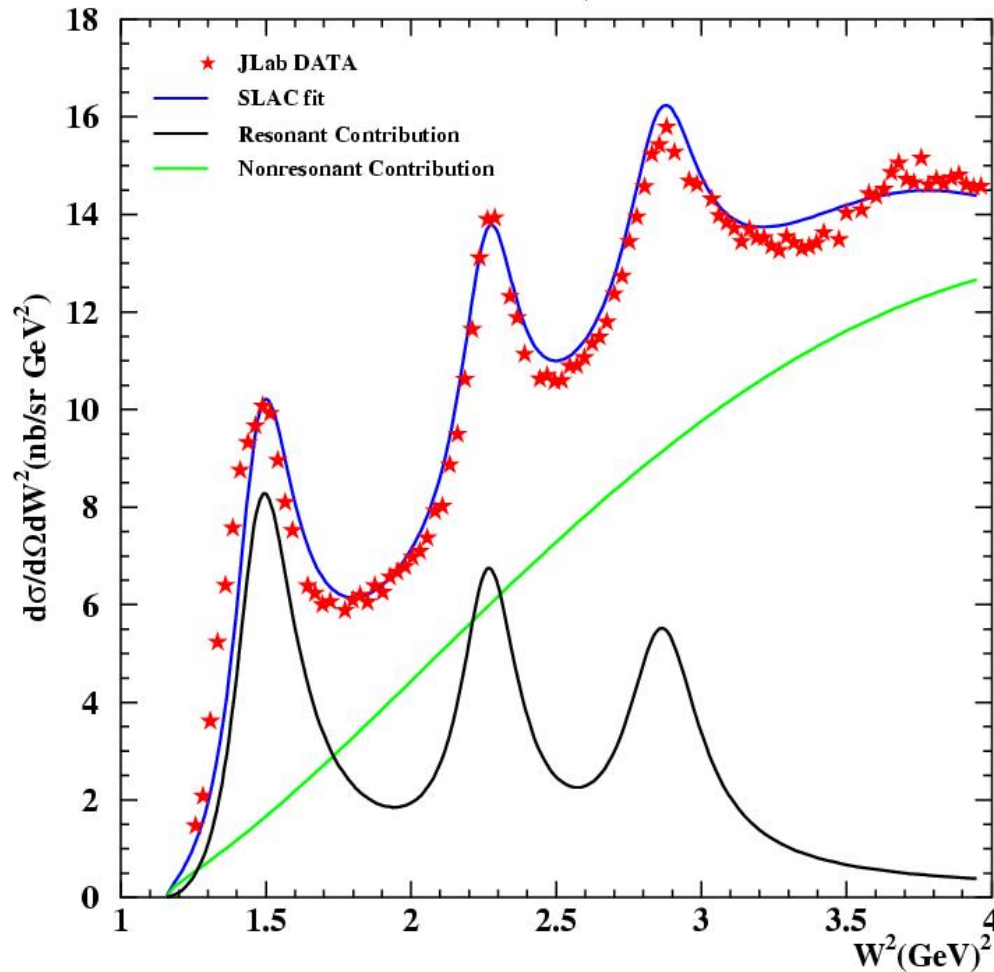
$$\frac{d\sigma}{d\Omega dE'} = \Gamma(\sigma_T + \varepsilon\sigma_L) = \Gamma\sigma_T(1 + \varepsilon R)$$

Or, in terms of structure functions $W_1(\nu, Q^2)$ and $W_2(\nu, Q^2)$:

$$\frac{d\sigma}{d\Omega dE'} = \frac{4\alpha^2 (E')^2}{Q^4} \left[W_2(\nu, Q^2) \cos^2 \frac{\theta}{2} + 2W_1(\nu, Q^2) \sin^2 \frac{\theta}{2} \right]$$

Inclusive ${}^1\text{H}(e, e')$ Scattering

$E = 3.245 \text{ GeV}, \theta = 26.98^\circ$



$$Q^2 = 4EE'\sin^2(\Theta/2)$$

$$\nu = E - E'$$

$$x = Q^2/(2M\nu)$$

$$W^2 = M^2 + 2M\nu - Q^2$$

$$= M^2 + Q^2(1/x - 1)$$

Define several regions:

0) elastic region: $W^2 = M^2$

1) 1st resonance excitation " Δ "

2) 2nd resonance region " S "

3) 3rd resonance region " F "

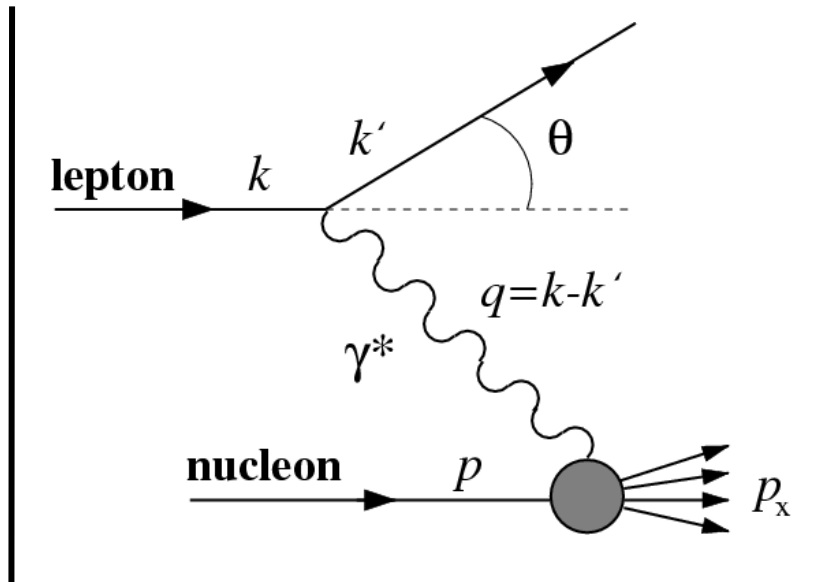
4) 4th region: $3.3 < W^2 < 4 \text{ GeV}^2$

5) Deep-inelastic " DIS " region

$W^2 > 4 \text{ GeV}^2$

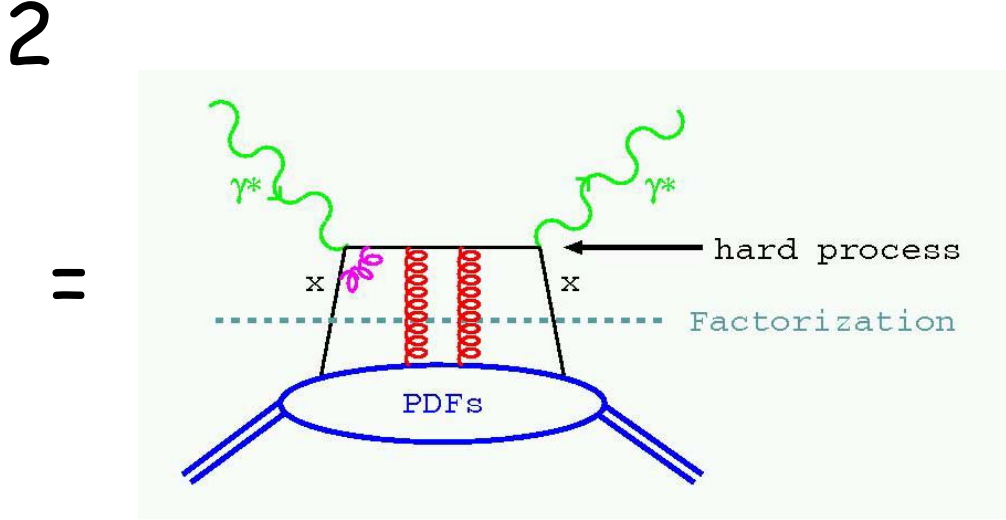
Spectrum consists of Resonant
and **Non-Resonant** Contributions

Deep Inelastic Scattering



Bjorken Limit: $Q^2 \rightarrow \infty, \nu \rightarrow \infty$

(Infinite Momentum Frame)



In the limit of large Q^2 , structure functions scale (with logarithmic corrections)

$$\begin{aligned}
 MW_1(\nu, Q^2) &\rightarrow F_1(x) \\
 \nu W_1(\nu, Q^2) &\rightarrow F_2(x)
 \end{aligned}
 \quad
 \mathbf{x} = \frac{Q^2}{2M\nu}$$

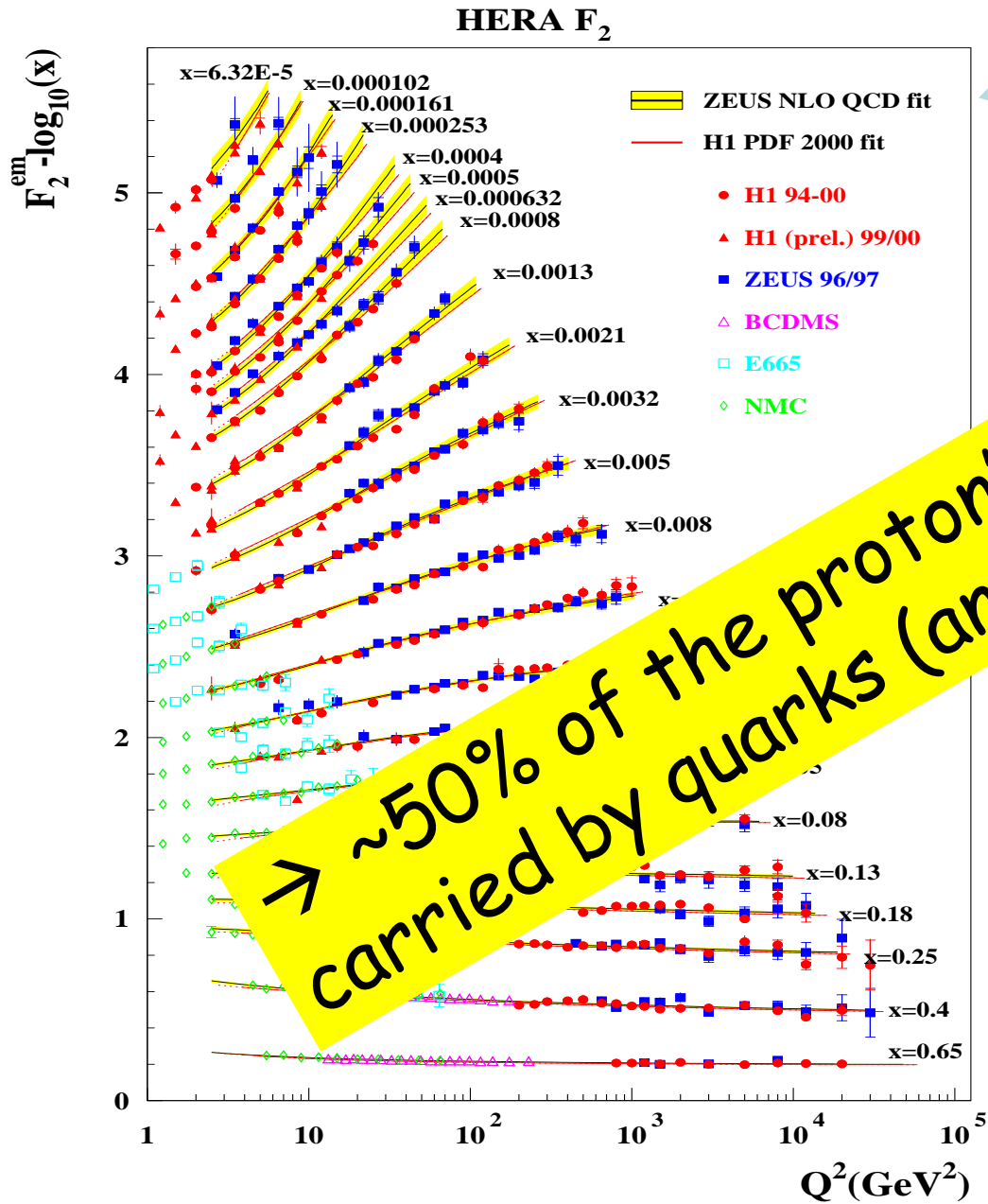
F_2 interpreted in the **quark-parton model** as the charge-weighted sum over quark distributions:

$$F_2(x) = \sum_i e_i^2 x q_i(x)$$

Empirically, DIS region is where logarithmic scaling is observed

$Q^2 > 1 \text{ GeV}^2, W^2 > 4 \text{ GeV}^2$

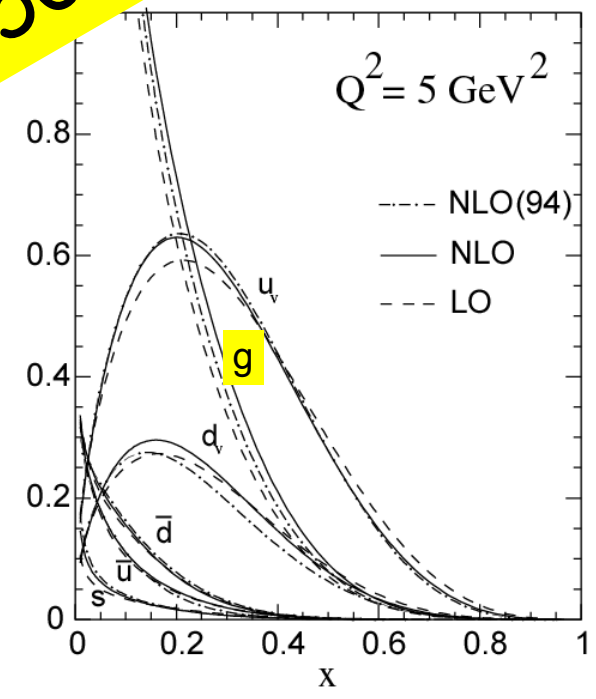
World Data on F_2^p Structure Function



(DIS data only)

In general, Next-to-Leading-Order (NLO) QCD (DGLAP) provides a good description of the data over the entire x range.

→ ~50% of the proton's momentum is carried by quarks (and ~50% by gluons)



Nuclear Physics in terms of protons, neutrons and pion exchange is a very good effective model.

Momentum transfer Q is negligible

Protons and Neutrons in terms of constituent (valence) quarks is a very decent effective model:
the Constituent Quark Model works surprisingly well.

Momentum transfer Q is small

Looking deep inside protons and neutrons, they are really balls of energy, with lots of gluons and quark-antiquark pairs popping in and out of existence.

Momentum transfer Q is "large"

The Quark Parton Model is well defined in the limit of large Q^2 and large ν (or W^2).

Empirically, deep inelastic scattering (or quark parton model) descriptions seem to work well down to modest energy scales: $Q^2 \sim 1 \text{ GeV}^2$, $W^2 \sim 4 \text{ GeV}^2$.

Why is the Quark-Hadron Transition in QCD so smooth, and occurring at such low energy scales?

The underlying reason is the **Quark-Hadron Duality** phenomenon.

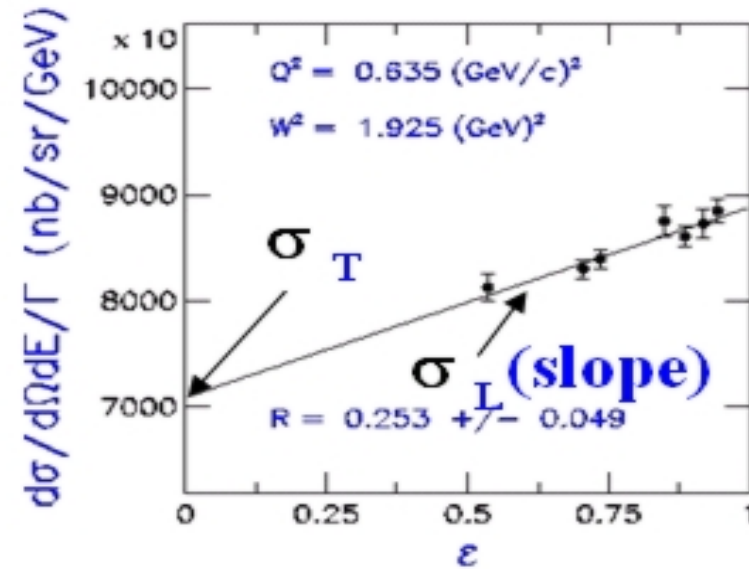


A Factory for "Rosenbluth" Separations

E.g.: Inclusive Scattering
 $e + p (d) \rightarrow e + X$

*Rosenbluth Separation
 Technique:*

$$\frac{d\sigma}{d\Omega dE'} = \Gamma(\sigma_T + \varepsilon\sigma_L)$$



Where: Γ = flux of transversely polarized virtual photons
 ε = relative longitudinal polarization

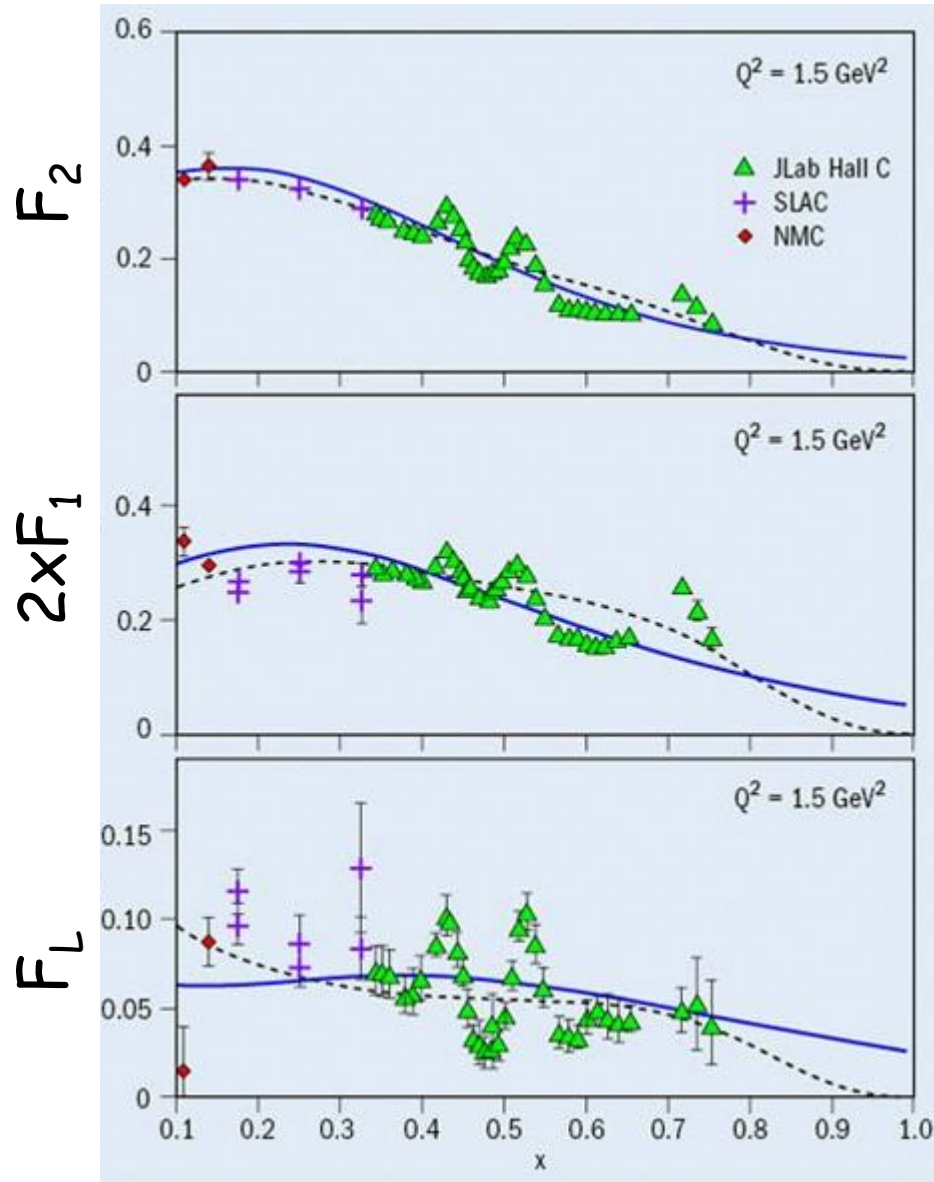
$$R = \frac{\sigma_L}{\sigma_T} = \frac{F_L}{2xF_1}$$

$$F_L = \left(1 + \frac{4M^2x^2}{Q^2}\right)F_2 - 2xF_1$$

longitudinal Transverse
m lx Ed

E94-110 : Separated Structure Functions

Duality works well for F_2 , $2xF_1$ (F_T), and F_L

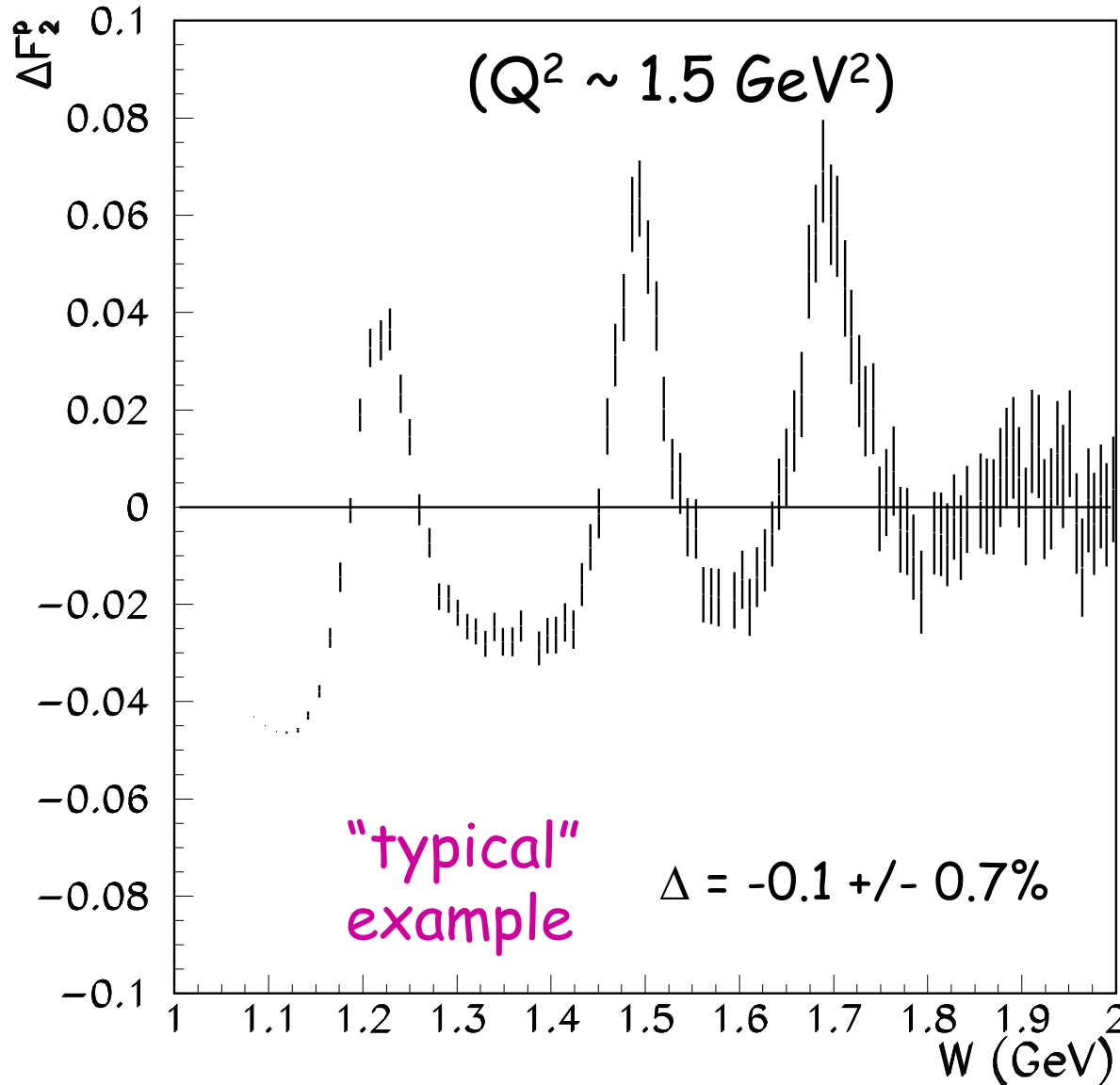


- The **resonance region** is, on average, well described by **NNLO QCD fits**.
- This implies that Higher-Twist (FSI) contributions cancel, and are on average small. **"Quark-Hadron Duality"**
- The result is a smooth transition from Quark Model Excitations to a Parton Model description, or a smooth quark-hadron transition.
- This explains the success of the parton model at relatively low W^2 ($=4 \text{ GeV}^2$) and Q^2 ($=1 \text{ GeV}^2$).

"The successful application of duality to extract known quantities suggests that it should also be possible to use it to extract quantities that are otherwise kinematically inaccessible."
(CERN Courier, December 2004)

Quantification: Resonance Region F_2 w.r.t. Alekhin NNLO Scaling Curve

$E=4$ GeV, $\theta=24$ Deg



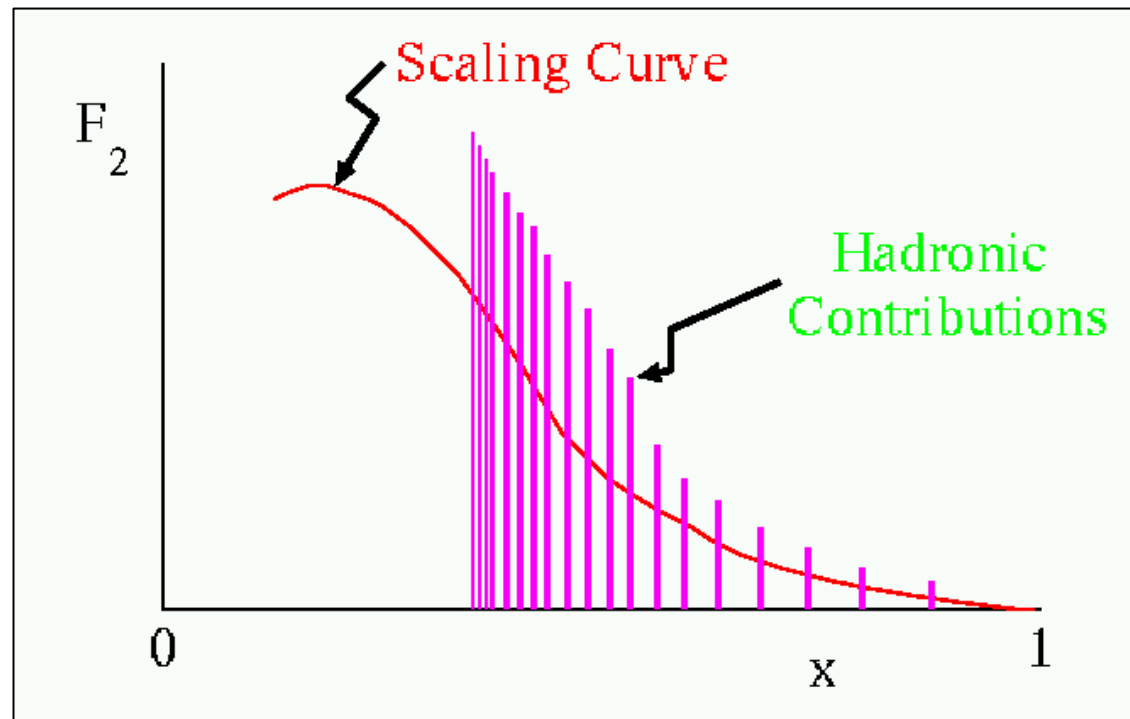
- Evidence of resonance transitions is "bumps and valleys" around the expected parton model behavior.
- Similar as standard textbook example of $e^+e^- \rightarrow \text{hadrons}$
- "Resonances build the parton subprocess cross section because of a separation of scales between hard and soft processes."
- Confinement is Local

Quark-Hadron Duality - Theoretical Efforts

N. Isgur et al : $N_c \rightarrow \infty$

$q\bar{q}$ infinitely narrow resonances

qqq only resonances



- Distinction between Resonance and Scaling regions is **spurious**
- Bloom-Gilman Duality must be invoked even in the Bjorken Scaling region → **Bjorken Duality**

QCD and the Operator-Product Expansion

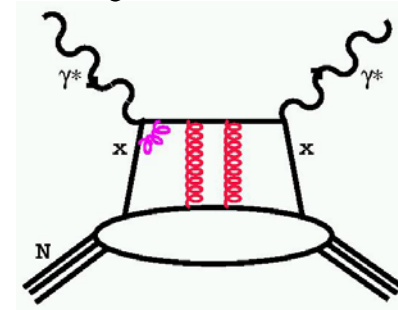
- Moments of the Structure Function
- Operator Product Expansion

$$M_n(Q^2) = \int_0^1 dx x^{n-2} F(x, Q^2)$$

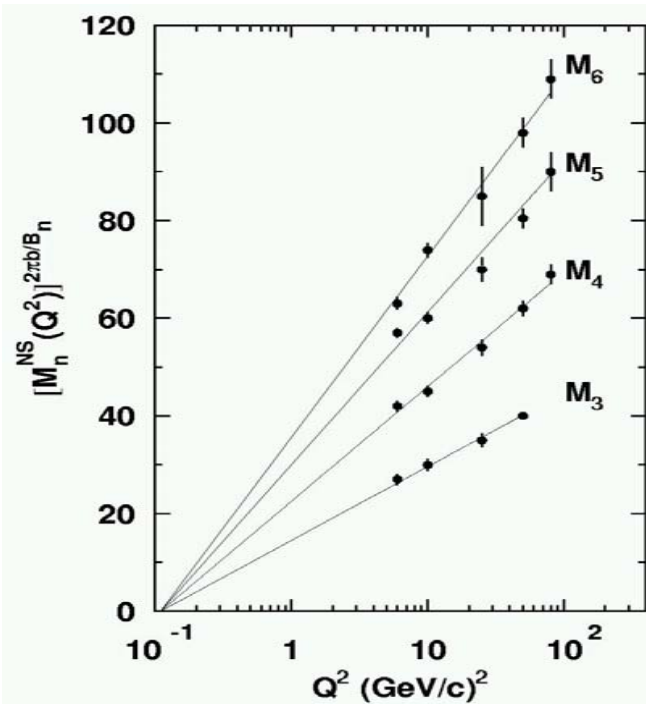
$$M_n(Q^2) = \sum_{k=1}^{\infty} (nM_0^2 / Q^2)^{k-1} B_{nk}(Q^2)$$

higher
twist

logarithmic
dependence



At High Q^2 : $\ln(Q^2)$ dependence of moments one of first "proofs" of QCD $\rightarrow \Lambda(QCD)$



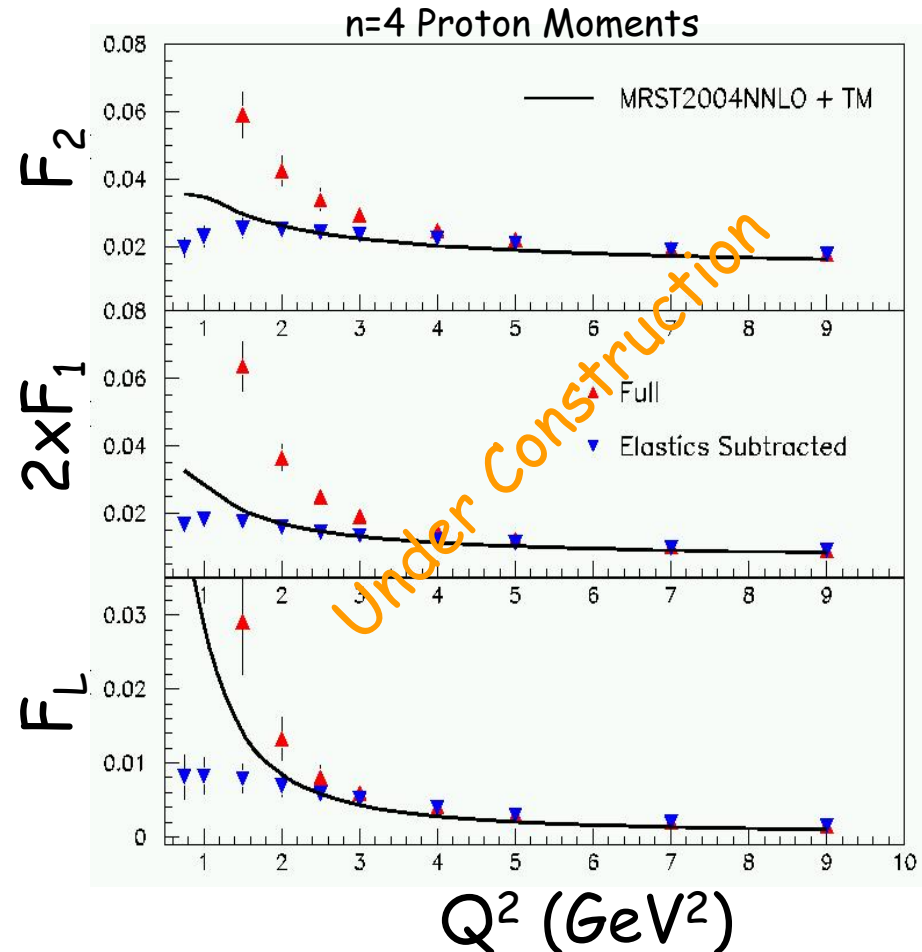
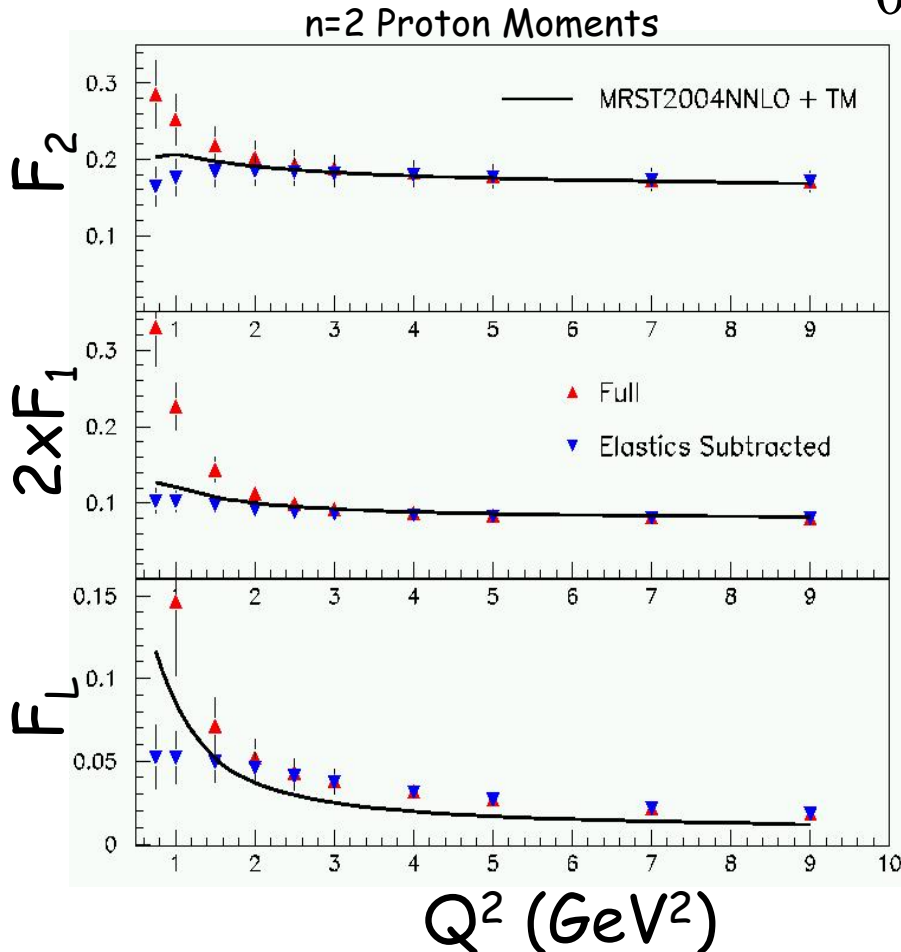
At Low Q^2 : $O(1/Q^2)$ power dependence is due to initial and final state interactions between the struck quark and target remnants

\rightarrow "Higher Twist" effects

Quark-Hadron Duality is described in the Operator Product Expansion *as higher twist effects being small or canceling*

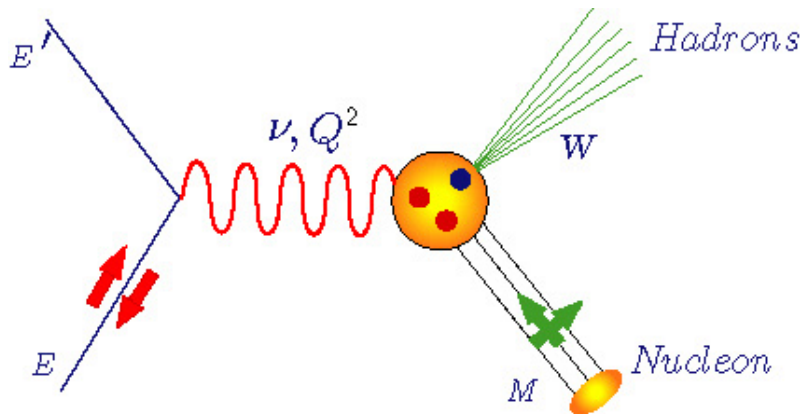
Separated Structure Function Moments up to $Q^2 = 4 \text{ GeV}^2$

$$M_n(Q^2) = \int_0^1 dx x^{n-2} F(x, Q^2)$$



- Higher-twist at low Q^2 mainly seems to reflect "discreteness" of low- W region
- $M_L^{(n)} = \alpha_s(Q^2) \left\{ \frac{4M_2^{(n)}}{3(n+1)} + \frac{2c \int dx x G(x, Q^2)}{(n+1)(n+2)} \right\}$ at leading twist and at zero proton-mass

Inclusive Electron Scattering - Formalism



Q^2 : Four-momentum transfer
 x : Bjorken variable ($=Q^2/2M\nu$)
 ν : Energy transfer ($\gamma = \nu/E$)
 M : Nucleon mass
 W : Final state hadronic mass

$$\text{U} \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow + \uparrow\uparrow) = \frac{8\alpha^2 \cos^2(\theta/2)}{Q^4} \left[\frac{F_2(x, Q^2)}{\nu} + \frac{2F_1(x, Q^2)}{M} \tan^2(\theta/2) \right]$$

- Unpolarized structure functions $F_1(x, Q^2)$ and $F_2(x, Q^2)$, or $F_T(x, Q^2)$ [$=2xF_1(x, Q^2)$] and $F_L(x, Q^2)$, to separate by measuring $R = \sigma_L/\sigma_T$
- Polarized structure functions $g_1(x, Q^2)$ and $g_2(x, Q^2)$

$$\text{L} \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\uparrow - \uparrow\uparrow) = \frac{4\alpha^2}{MQ^2} \frac{E'}{\nu E} \left[(E + E' \cos \theta) g_1(x, Q^2) - \frac{Q^2}{\nu} g_2(x, Q^2) \right]$$

$$\text{T} \quad \frac{d^2\sigma}{dE'd\Omega}(\downarrow\Rightarrow - \uparrow\Rightarrow) = \frac{4\alpha^2 \sin \theta}{MQ^2} \frac{E'^2}{\nu^2 E} \left[\nu g_1(x, Q^2) + 2E g_2(x, Q^2) \right]$$

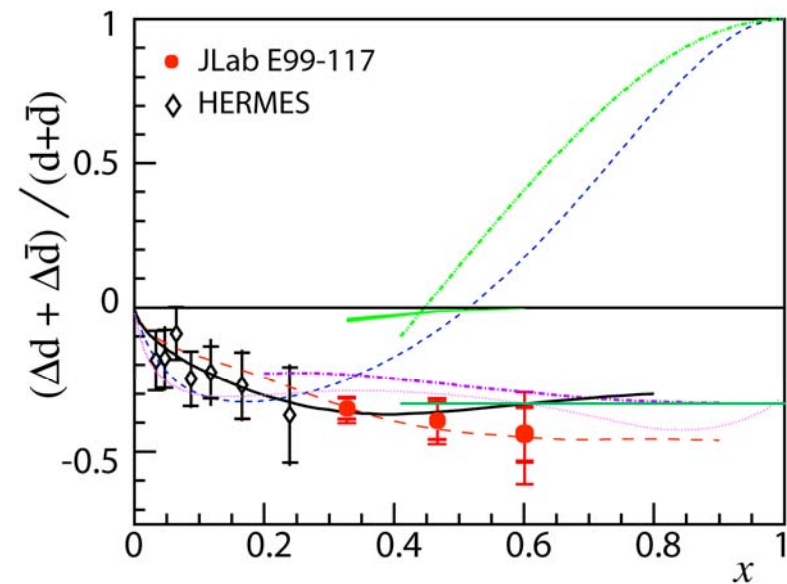
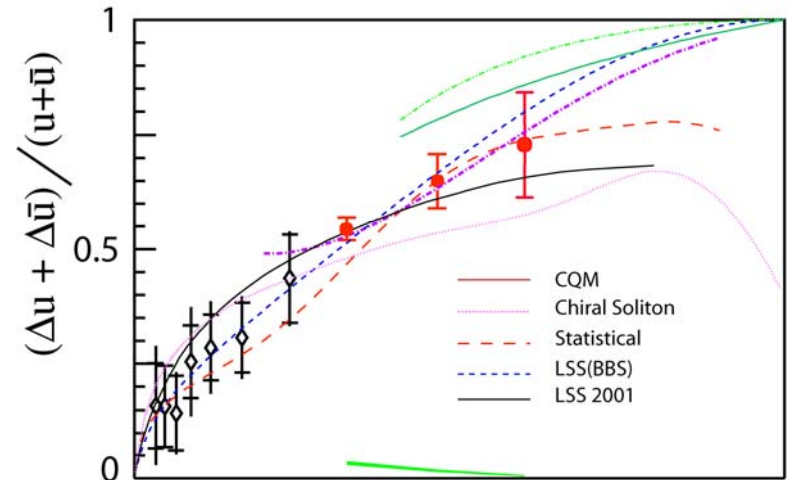
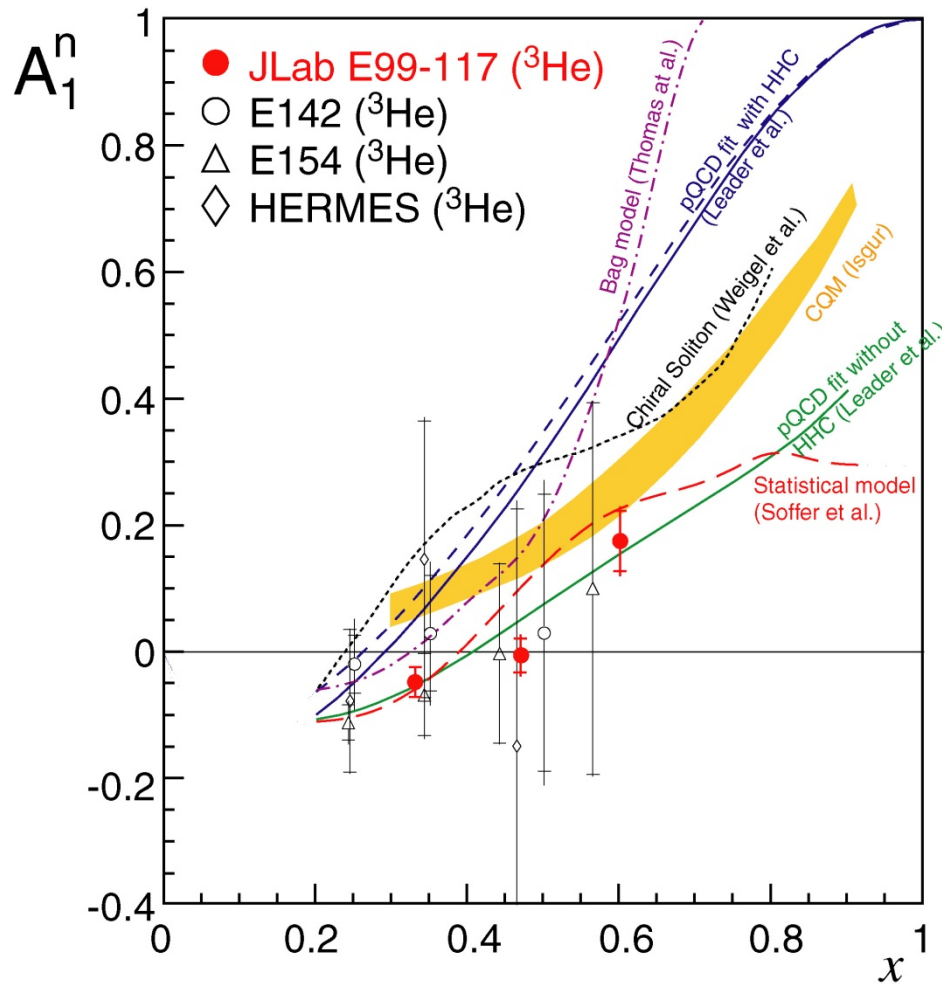
Parton Model Ideas Valid @ 6 GeV

Hall A

First measurement in large- x region unambiguously showing that $A_1^n > 0$ ($A_1^n = 0$ in the SU(6) Quark Model)



Allows for Flavor Decomposition:



Structure function g_1 and its $\Gamma_1(Q^2)$ Moment

$$\Gamma_1(Q^2) = \int_0^1 g_1(x, Q^2) dx$$

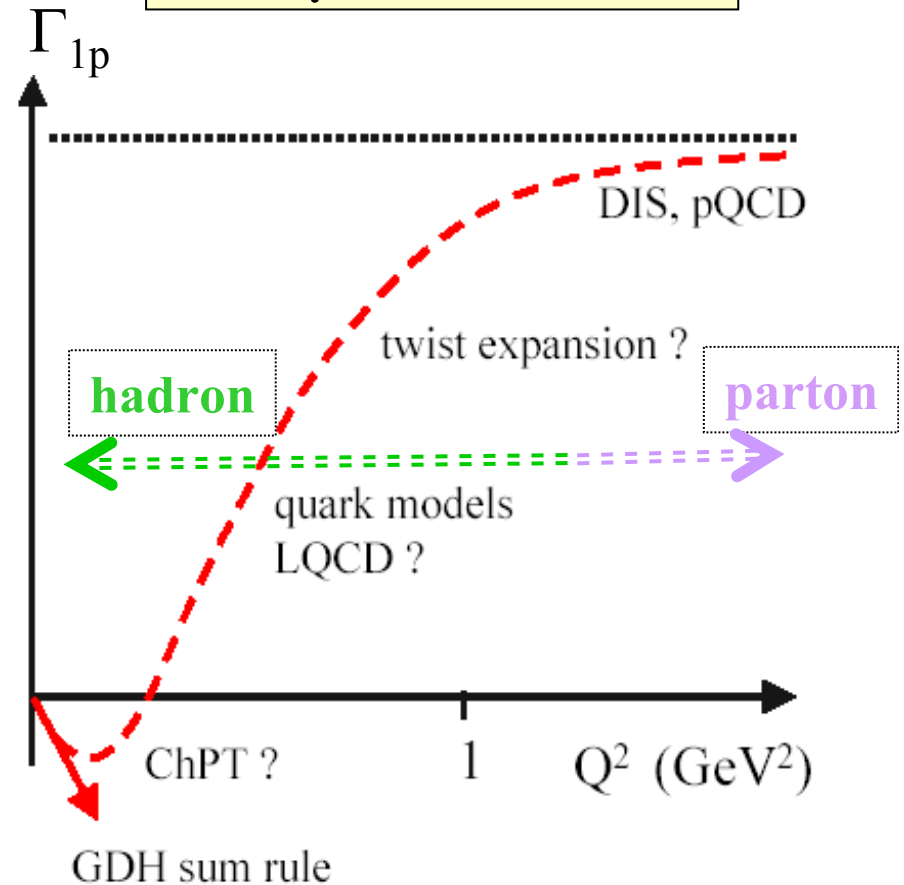
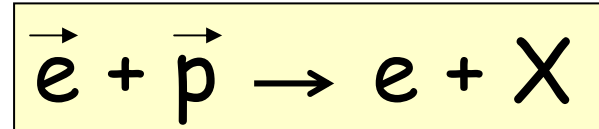
As $Q^2 \rightarrow \infty$, isospin symmetry and current algebra lead to the **Bjorken sum rule**, relating the n-p difference to the **neutron β -decay coupling constant g_A**

$$\Gamma_1^p - \Gamma_1^n = g_A/6$$

As $Q^2 \rightarrow 0$, Lorentz invariance, unitarity, and dispersion relations lead to the **GDH sum rule**, relating it to the **anomalous magnetic moment of the nucleon**

$$\Gamma_1 \xrightarrow{Q^2 \rightarrow \infty} \frac{Q^2}{2M^2} \bigg|_{\text{GDH}}$$

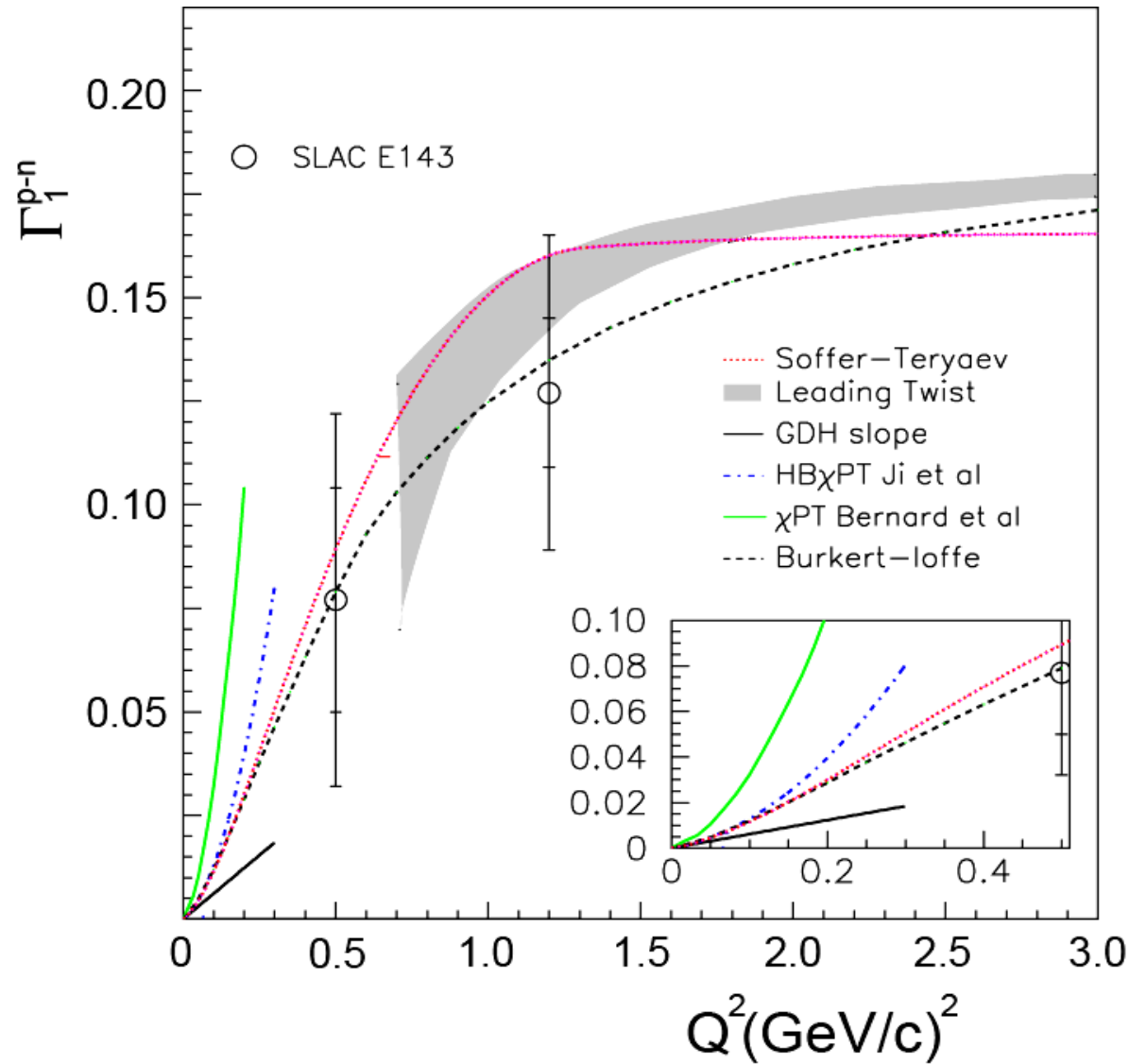
Expect rapid change of Γ_1 in transition from the hadronic to the partonic regimes.



"Zoom in" from tiny length scales (DIS) to large length scales

Bjorken Integral Γ_1^{p-n} (pre-JLab)

Impressive set of data at larger Q^2 (not shown) validates Bjorken Sum Rule to ~10-15%.



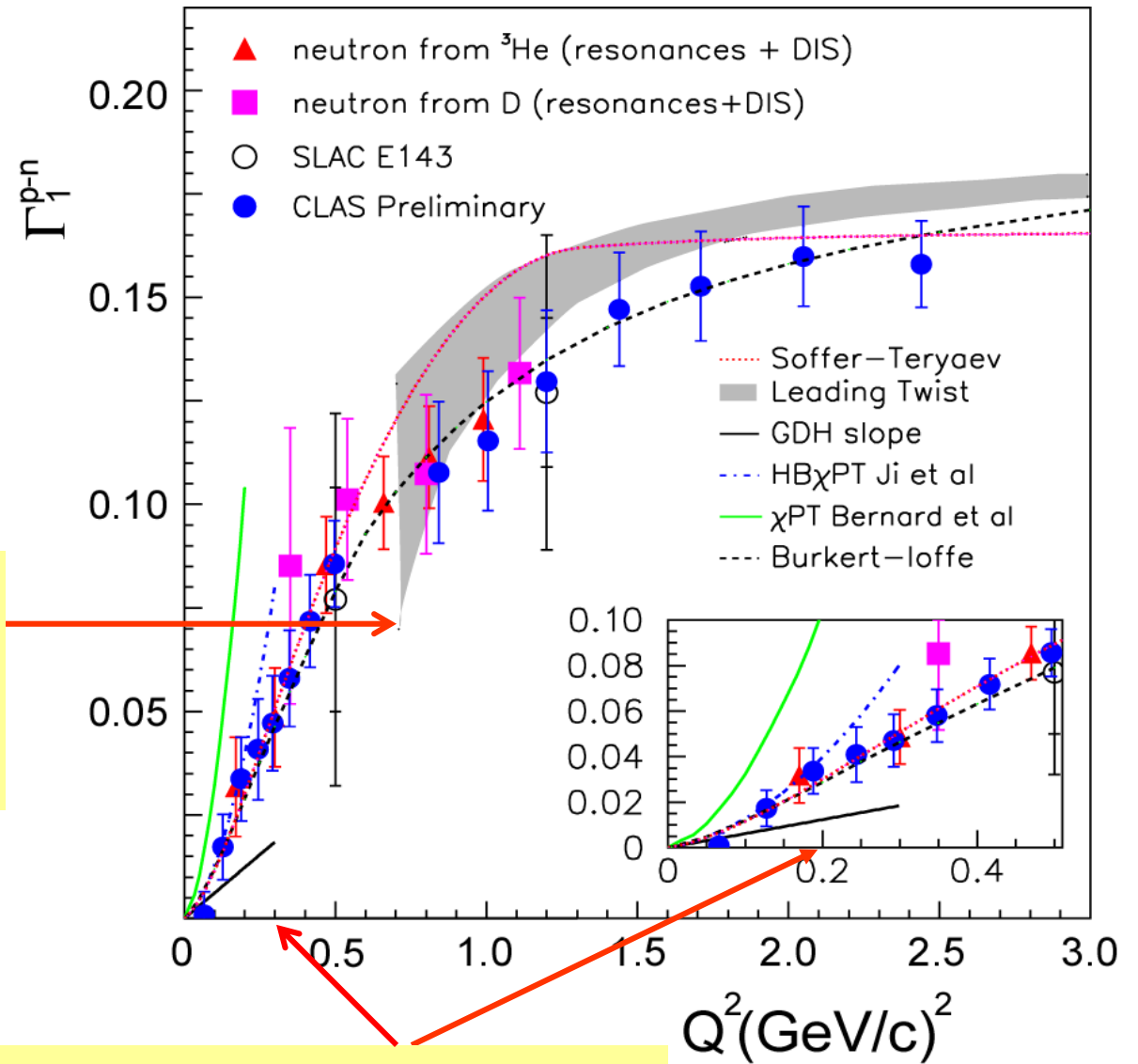
Bjorken Integral Γ_1^{p-n} (today)

Hall B

Hall A

Operator Product Expansion description works surprisingly well for $Q^2 > 0.7 \text{ GeV}^2$.

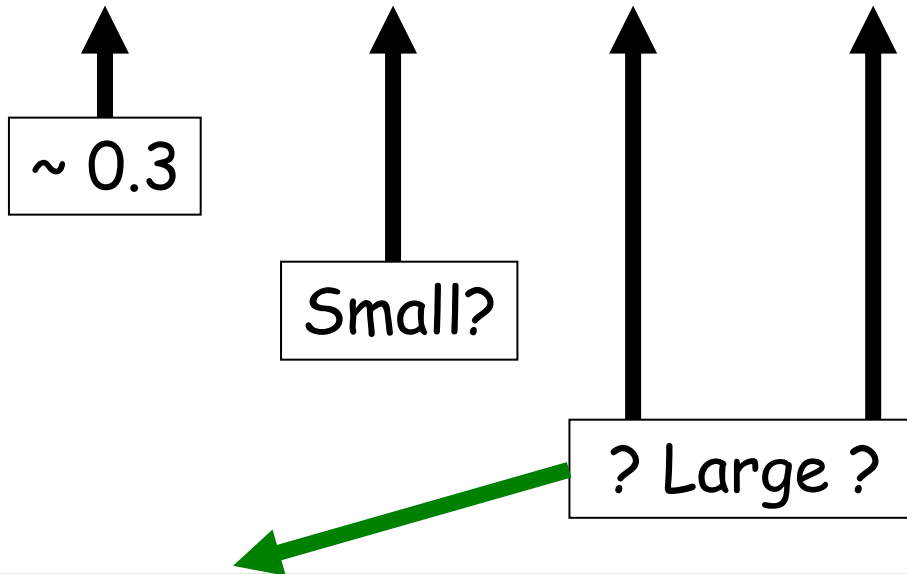
HB χ PT compatible for $Q^2 < 0.2 \text{ GeV}^2$



The Spin Structure of the Proton

Proton helicity sum rule:

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_q + L_g$$



The Impact of Quark and Gluon Motion on the Nucleon Spin

"TMDs and GPDs"

10 Years of Physics Experiments at JLab

- Experiments have successfully addressed original Mission Statement:
“The study of the largely unexplored transition between the nucleon-meson and the quark-gluon descriptions of nuclear matter”
Highlight 1: The Role of Quarks in Nuclear Physics
Probing the Limits of the Traditional Model of Nuclei
- Emphasis has slowly shifted from Base Equipment Experiments to Experiments with dedicated/additional setups and/or detectors
- Emphasis has shifted to third sub-area of intended CEBAF research:
“What are the properties of the force which binds quarks into nucleons and nuclei at distances where this force is strong and the quark confinement mechanism is important?”
- *Highlight 2: Charge and Magnetization in Nucleons and Pions*

Charge distribution in proton differs from magnetization distribution
Elusive charge distribution of neutron well mapped out to high resolution
Strange quarks play <5% role in mass of proton → unsolved mysteries...

- *Highlight 3: The Onset of the Parton Model at Low Energies*

High quality hadronic structure function data at JLab at 6 GeV have been accumulated spanning the nucleon resonance and low- W^2 deep inelastic region. The data indicate a surprisingly smooth parton-hadron transition at relatively low Q^2 , allowing, for $x > 0.1$, an unprecedented access to Parton Model physics with the 12 GeV Upgrade